

DIRDOP: a directivity approach to determining the seismic rupture velocity vector

Bento Caldeira · Mourad Bezzeghoud · José F. Borges

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Abstract Directivity effects are a characteristic of seismic source finiteness and are a consequence of the rupture spread in preferential directions. These effects are manifested through seismic spectral deviations as a function of the observation location. The directivity by Doppler effect method permits estimation of the directions and rupture velocities, beginning from the duration of common pulses, which are identified in waveforms or relative source time functions. The general model of directivity that supports the method presented here is a Doppler analysis based on a kinematic source model of rupture (Haskell, Bull Seismol Soc Am 54:1811–1841, 1964) and a structural medium with spherical symmetry. To evaluate its performance, we subjected the method to a series of tests with synthetic data obtained from ten typical seismic ruptures. The experimental conditions studied correspond with scenarios of simple and complex, unilaterally and bilaterally extended ruptures with different mechanisms and datasets with different levels of azimuthal coverage. The obtained results generally agree with the expected values. We also present four real case studies, applying the

method to the following earthquakes: Arequipa, Peru ($M_w = 8.4$, June 23, 2001); Denali, AK, USA ($M_w = 7.8$; November 3, 2002); Zemmouri–Boumerdes, Algeria ($M_w = 6.8$, May 21, 2003); and Sumatra, Indonesia ($M_w = 9.3$, December 26, 2004). The results obtained from the dataset of the four earthquakes agreed, in general, with the values presented by other authors using different methods and data.

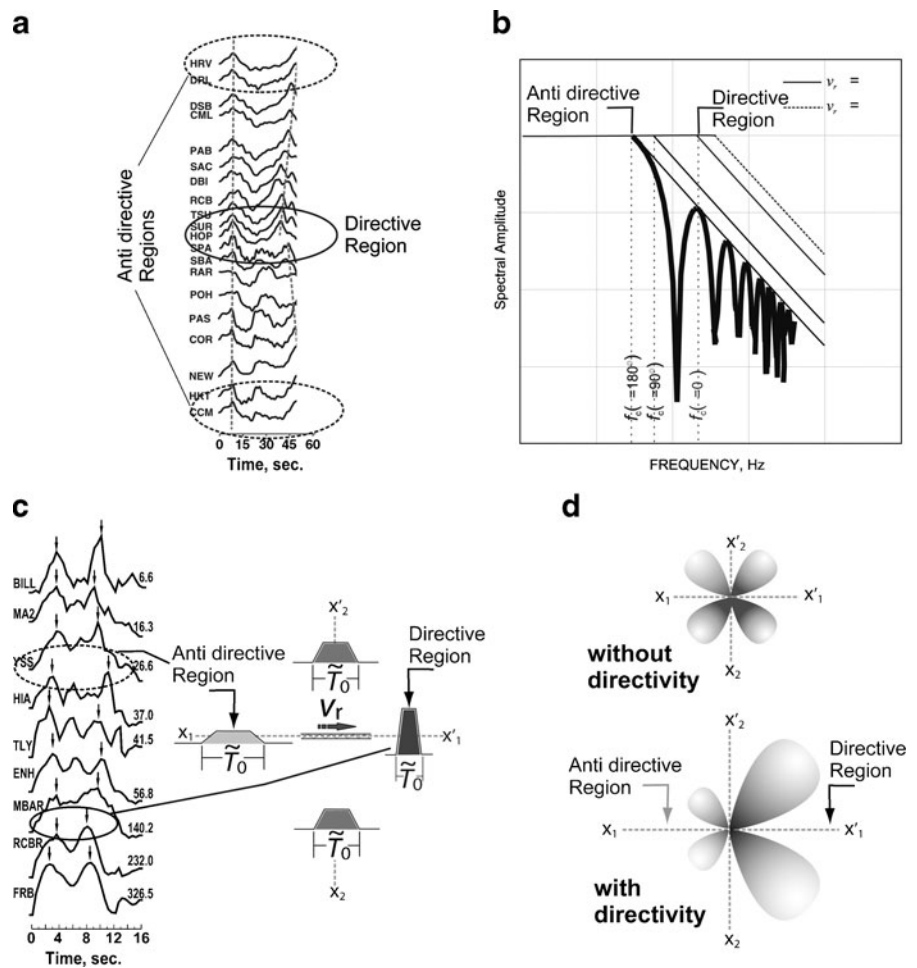
Keywords Directivity · Doppler effect · Seismic source · Rupture parameters · Inversion

1 Introduction

The radiation that issues from an extended seismic source when a rupture spreads in preferential directions has characteristics that distinguish it from the radiation emitted by a point source (Benioff 1955). These distinctive characteristics, which are known as directivity (Ben-Menahem 1961), are manifested by an increase in the frequency and amplitude of seismic waves when the rupture occurs in the direction of the seismic station and a decrease in the frequency and amplitude if it occurs in the opposite direction. Moreover, these effects are not present when the rupture's direction is perpendicular to the propagation direction. Evidence of this behavior is found in a multiplicity of seismic observations (Fig. 1), including the

B. Caldeira (✉) · M. Bezzeghoud · J. F. Borges
Centro de Geofísica de Évora (CGE)
e Departamento de Física,
Universidade de Évora, Évora, Portugal
e-mail: bafcc@uevora.pt

Fig. 1 Effects of rupture directivity: **a** common pulse duration at different azimuths from the rupture, **b** corner frequency variation on spectra diagrams of body wave displacement, **c** pulse duration variation observed in relative source time functions, and **d** symmetric change of the radiation pattern with maximum amplitude related to the direction of the rupture



following: (a) a variation of pulse duration observed in waveforms at stations with differing azimuths (e.g., Fukao 1972; Tibi et al. 1999; Caldeira et al. 2004), (b) variations of corner frequencies observed in the amplitude spectra (e.g., Tumarkin and Archuleta 1994; Hoshiba 2003), (c) pulse duration variations observed in relative source time functions (RSTF; e.g., Ihmlé 1998; Baumont et al. 2002; Kraeva 2004), and (d) symmetric changes of the radiation pattern in which the maximum amplitude is related to the direction of the rupture (e.g., Benioff 1955; Ben-Menahem and Singh 1981; Kasahara 1981).

The term directivity that is associated with spectral deviations caused by finite moving sources was first used by Ben-Menahem (1961),

who quantified it with the directivity function $D_\theta(\omega)$. This function is defined as the ratio of the spectral displacements from two places that are diametrically opposite from the focus. Considering a kinematic model of rupture propagation, as in Haskell (1964), and a homogeneous and isotropic medium, the zeros of the directivity function occur at frequencies

$$\omega_n (D = 0) = \frac{2n\pi}{\tilde{T}_0(\theta)}, \quad (n = 1, 2 \dots), \quad (1)$$

where $\tilde{T}_0(\theta)$ is the apparent source rupture time observed at a station whose relation to the

epicenter defines an angle θ with the direction of the rupture. $\tilde{T}_0(\theta)$ is written in the form

$$\tilde{T}_0(\theta) = \frac{L}{v_r} - \frac{L}{c} \cos \theta, \quad (2)$$

where L is the rupture length, v_r the rupture velocity, and c the phase velocity of the wave (P or S).

The apparent rupture time $\tilde{T}_0(\theta)$ is the result of two terms: L/v_r , which represents the real source duration, i.e., the rupture time when measured in its own referential, and $-(L/c) \cos \theta$, which expresses the delay relative to the real rupture time. This term is a function of the observation direction.

These directivity effects are believed by some authors to be equivalent to the Doppler effect (e.g., Ben-Menahem and Singh 1981; Douglas et al. 1988; Velasco et al. 2004); however, this interpretation is not unanimously accepted. For example, Aki and Richards (1980) and Bullen and Bolt (1985) found the two effects to be different, although they do recognize analogies between them. Aki and Richards (1980), for example, pointed out that the amplitude variations caused by destructive interference between the waves originating from different positions on the fault are a distinctive feature of seismic directivity. According to them, this feature clearly shows the difference between the two effects. The Doppler effect, in its classical formulation, is in fact limited to a single oscillation. Douglas et al. (1988) compare the theoretical models of the Doppler effect and seismic directivity and show that, in both cases, the equations are identical although they are ascertained differently. They concluded that it is appropriate to associate Doppler's name with the effect of the variation in pulse shape due to a moving seismic source. The polychromatic nature of the source does not fundamentally invalidate the applicability of the Doppler analysis. Some similar problems occur in other scientific areas, involving multifrequency oscillators that are also known as Doppler (e.g., Loupas and Gill 1994; Grach et al. 1997; Russell and Brucher 2002; Rao et al. 2009).

Although seismic directivity is recognized unanimously as being characteristic of extended sources and as a function of some important

source parameters, such as length, rupture direction, rupture velocity, and rupture time, it is not a widely studied subject. Its use in determining source parameters from seismic records has been developed in two ways:

- (a) The first method, based on the directivity function of Ben-Menahem (1961) (e.g., Ben-Menahem and Singh 1981; Udias 1971; Pro 2002; Pro et al. 2007), consists of finding the length of the source and the rupture velocity that produces a good visual fit between the synthetic and observed diagrams of the directivity function calculated using surface waves. This method requires knowledge of the rupture azimuth and pairs of records acquired at equidistant and diametrically opposite locations from the source. These requirements are always difficult to satisfy. Pro (2002), on the other hand, developed a method that allows pairs of data to be used although they are not from exactly opposite locations. She also used a method based on the first minima of Eq. 1 to decide which planes of the focal mechanism correspond to the rupture.
- (b) The second approach uses the apparent duration of the rupture gathered from seismic waveforms or from the apparent source time functions, which are both azimuthally distributed. Equation 2 is then applied to estimate the parameters of source finiteness (e.g., Fukao 1972; Boore and Joyner 1978; Cipar 1979; Beck et al. 1995; Ihmlé 1998; Tibi et al. 1999; Kraeva 2004)

In this study, we use a similar scheme to determine the direction and rupture velocity and the corresponding errors. The directivity by Doppler effect (DIRDOP) program uses time delays between common pulses selected in broadband seismic body waves with an azimuthal distribution around the epicenter; it calculates the source parameters through a subsequent Doppler analysis.

To evaluate the program, we applied it to a set of synthetic data from typical scenarios of seismic ruptures. Finally, to test the program on a real situation, we applied it to four earthquakes: Arequipa, Peru ($M_w = 8.4$, June 23, 2001); Denali, AK, USA ($M_w = 7.8$, November 3, 2002);

Zemmouri–Boumerdes, Algeria ($M_w = 6.8$, May 21, 2003); and Sumatra, Indonesia ($M_w = 9.3$, December 26, 2004).

2 Theory

The rupture process of an extended seismic source can be viewed as a sequence of shocks due to rapid slips, which are produced along certain fault paths. Each shock causes vibrations that spread in all directions of the Earth's interior following the laws of seismic wave propagation theory.

According to this model, the seismic record at any point on the earth's surface contains a signature of the rupture process that originated the recorded waveform. It is possible, by comparing several readings of waveforms azimuthally distributed from the source, to analyze the Doppler effect, so as to determine the direction and velocity of the rupture. In general, the physical phenomenon known as the Doppler effect occurs whenever a wave's source moves relative to an observer. It is revealed by variations in the frequencies recorded by observers distributed at different points in relation to the source.

When the source moves with a rupture velocity v and emits wave pulses that propagate in a homogeneous and isotropic medium with a constant phase velocity c , the Doppler effect can be mathematically expressed (French 1974) as

$$\Delta\tau = \Delta\tau_0 \left(1 - \frac{v \cos \theta}{c} \right), \quad (3)$$

where $\Delta\tau_0$ is the time delay between two pulses measured in the source referential, $\Delta\tau$ is the equivalent time delay measured at a fixed position that forms an angle θ with the direction of movement from the source, and c is the phase velocity of the wave in the medium. Equation 3 shows that the measurement performed by an external observer depends on the source component velocity in the incidence direction of the wave, $v \cos \theta$. Any application of this effect should take into account this rule, i.e., that the second term of Eq. 3 is the ratio between the components of source velocity in the wave incidence direction and its phase velocity. After the necessary modifications for the propagation of seismic rays in a

spherically layered medium, the following is the equivalent equation that relates the measurement of the time delay between two shocks that occur at the source with an interval $\Delta\tau_0$ spread with a constant velocity v_r , with the corresponding time delay $\Delta\tau_j$ measured at station j :

$$\Delta\tau_j(\theta, i) = \Delta\tau_0 \left(1 - \frac{v_{rH} \sin i_j \cos \theta_j}{c} \right). \quad (4)$$

Here, v_{rH} is the horizontal component of the rupture velocity and i_j is the incidence angle at the j -th observation location. Inserting the slowness parameter p into Eq. 4, the equation becomes

$$\Delta\tau_j(\theta, p) = \Delta\tau_0 \left(1 - \frac{p_j v_{rH} \cos \theta_j}{R_0} \right), \quad (5)$$

where R_0 is the Earth's radius. According to Eq. 5, $\Delta\tau_j$ depends on two variables: the distance from the source (p_j/R_0) and the angle between the rupture direction and the station position (θ_j). The spatial distribution of $\Delta\tau_j$ is schematically represented in Fig. 2. According to Eq. 5, $\Delta\tau_j$

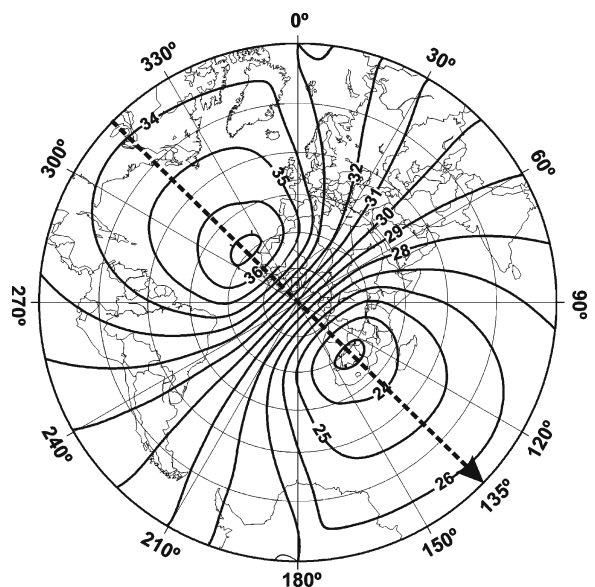


Fig. 2 Theoretical spatial distribution (isolines) of common pulses (time delays) measured on seismograms obtained from an extended seismic source located at latitude = 0°, longitude = 0°. The rupture propagates with a constant velocity, $v_r = 3.0$ km/s, toward N135E. In the source, we considered a 30-s time pulse, which is the value read from seismograms in directions perpendicular to the rupture

for equidistant positions from the focus is minimal for $\theta = 0^\circ$, that is, in positions aligned with the direction of rupture progression, and has the value $\Delta\tau_0$ at positions perpendicular to the rupture direction. Thus, by examining the azimuthal distribution of apparent time delays, $\Delta\tau_j(\theta, p)$, it is possible to evaluate the direction of the rupture.

Calculating the rupture velocity requires careful analysis. In reality, the data frequently come from restricted and poorly distributed observation points in azimuth, as well as distance. Because of this, diagrams constructed with real data, such as Fig. 2, do not explicitly define the rupture direction. For the same reason, estimates of v_{rH} calculated using these data can also be imprecise. This difficulty can be overcome by normalizing measures to a standard value p_0 of slowness. The normalization transforms the equation of two variables, Eq. 5, into one involving only one variable,

$$\Delta\tau_j^*(\theta) = \Delta\tau_0 \left[1 - v_{rH} \left(\frac{p_0}{R_0} \right) \cos \theta_j \right], \quad (6)$$

where $\Delta\tau_j^*$ are the normalized time delays. Figure 3 represents the time delays normalized to a distance of 30° , $\Delta\tau_j^*$, as a function of the azimuth of the observation locations θ .

According to Eq. 6, the minimum of $\Delta\tau^*$, $\Delta\tau_{\min}^*$, is measured at an observation location that defines the direction of v_{rH} , an angle $\theta_j = 0$. On the other hand, at the points orthogonal to that direction ($\theta_j = 90^\circ$), $\Delta\tau^* = \Delta\tau_0$. Finally, with these two pa-

rameters, $\Delta\tau_{\min}^*$ and $\Delta\tau_0$, obtained from the curves (see Fig. 3), we can calculate v_{rH} :

$$v_{rH} = \frac{1 - (\Delta\tau_{\min}^* / \Delta\tau_0)}{p_0 / R_0} \quad (7)$$

The normalization procedure consists of calculating the correction parameter χ_j , which provides the measurements at the standard distance for each observation point, using

$$\Delta\tau_j^*(\theta) = \Delta\tau_j(\theta, p) \chi_j, \quad (8)$$

where the normalization parameter is given by

$$\chi_j = \frac{1 - v_{rH} \left(\frac{p_0}{R_0} \right) \cos \theta_j}{1 - v_{rH} \left(\frac{p_j}{R_0} \right) \cos \theta_j}. \quad (9)$$

The calculation of v_{rH} from Eqs. 7, 8, and 9 is a nonlinear inverse problem that we can solve numerically using an iterative nonlinear least-squares method (Menke 1984). Because the distribution of the data is assumed to be Gaussian, the errors of velocity and azimuth of rupture are calculated from the covariance matrix of inverted parameters.

The method, as it was used, calculates the horizontal component of the rupture velocity v_{rH} ; the rupture velocity v_r , on the other hand, can be estimated if the geometric fault parameters (strike = ϕ and dip = δ) are known. For the geometry shown in Fig. 4, the rupture velocity is given by

$$v_r = \frac{v_{rH}}{\cos \delta} \sqrt{\cos^2 \psi \cos^2 \delta + \sin^2 \psi} \quad (10)$$

Fig. 3 Azimuthal distribution of the pulses represented in Fig. 2 to a normalized distance of 30° , which corresponds to $p_0 / R_0 = 0.08$ s/km. The minimum of the curve occurs in the direction of the rupture and the maximum in the opposite direction

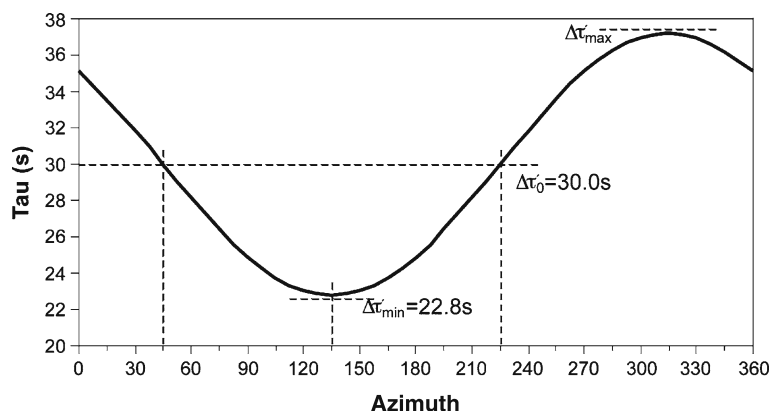
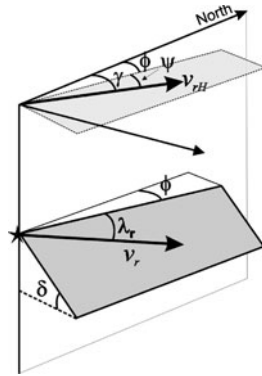


Fig. 4 Description of the geometric parameters used to represent the fault orientation with (*top*) and without (*bottom*) projection on the surface



and the rupture direction on the fault plane by

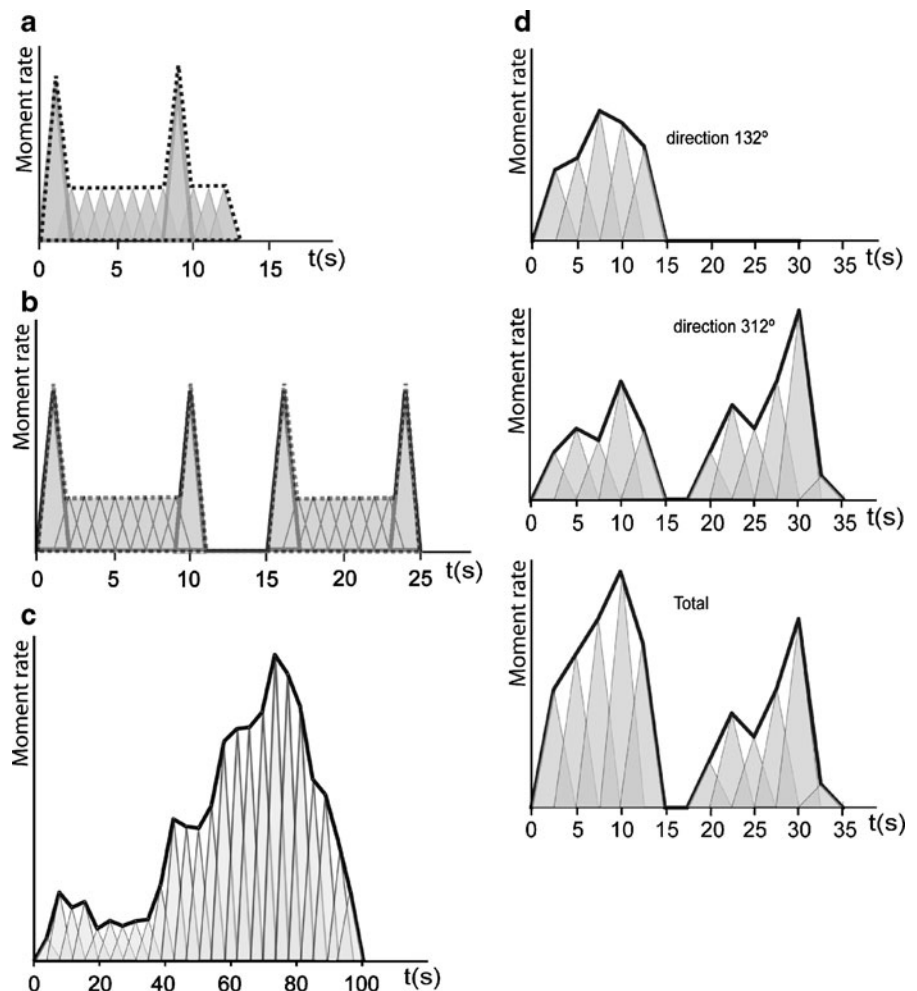
$$\lambda_r = \arctan \left(\frac{\tan \psi}{\cos \delta} \right), \tag{11}$$

where $\psi = \gamma - \phi$.

The procedure described above establishes the DIRDOP approach that allows for calculation of the rupture direction and velocity for extended seismic sources using the common pulses identified on seismograms of stations distributed around the source. Consider the special case of a unilateral rupture with constant velocity, as described in the kinematic Haskell model. If, in each seismogram, a delay interval, $\Delta\tau_j$, is selected that corresponds to the difference between the initial and final pulse times of the rupture, $\Delta\tau_j(\theta, p) = \tilde{T}_0(\theta, p)$, the apparent rupture time. In this case, $\Delta\tau_0 = L/v_r$, where L is the rupture length. Under these conditions, the application of DIRDOP to this particular case (Eq. 5) becomes

$$\tilde{T}_0(\theta, p) = \frac{L}{v_r} - \frac{pL}{R_0} \cos \theta. \tag{12}$$

Fig. 5 Source time functions (STF) used to generate the synthetic waveforms of the extended ruptures. The STF is the sum of narrow triangular functions (rise time of 1 s) with different amplitudes at regular time intervals. The highest *triangles* produce stronger visual marks on the synthetic seismograms, making the corresponding pulses more easily identifiable. In **a**, the STF used is associated with unilateral ruptures (scenarios S1, S2, S3, S4, and S5); in **b**, the STF used is related to a bilateral rupture (scenario S6); **c** STF similar to the Arequipa (Peru), June 23, 2001 earthquake, used to generate the complex unilateral ruptures C1, C3, and C4; and **d** STF used to generate the bilateral rupture C2



Equation 12 defines the apparent source time rupture as a function of the observation point. An identical equation can be deduced by integrating the Haskell (1964) rupture model applied to a layered spherical structure model (Fukao 1972; Caldeira 2004).

3 Evaluation of the method

To evaluate this methodology, we applied it to a set of typical synthetic scenarios of seismic ruptures. This kind of evaluation with synthetic data is extremely important because it represents the only way to analyze the performance of the methods because the expected results are known (Beresnev 2003).

3.1 Synthetic data

The data used were obtained from synthetic seismograms generated by Borges' (2003) KIKDIR-REC program. This program is based on the seismic source model of Kikuchi and Kanamori (1991), which synthesizes the displacement, u_j , produced at any point on the Earth's surface due to an extended seismic rupture in its interior. The rupture is defined by a succession of point sources distributed on a rectangular fault characterized

by the parameters φ (strike) and δ (dip; Fig. 4). Each subevent is characterized by a triangular source time function (STF) with rise time τ and a slip vector defined by an angle λ (rake). The rupture velocity is defined using the position and occurrence time of each point source, which in turn are defined by the three parameters ΔD , Δt , and λ_r , which represent the distance between subevents, the time interval between subevents, and the rupture direction on the fault, respectively. The complete STFs (Fig. 5) are defined by a sequence of partially overlapping triangular functions. The structure model used to calculate the Green functions was the ISASP91 model of Kennett and Engdahl (1991).

Ten scenarios (defined in Table 1) were tested. The first six, with the denomination S (from 1 to 6), correspond to a very simple STFs (Fig. 5a, b); the last four, with the denomination C (from 1 to 4), correspond to STSs representative of the complexity observed in real earthquakes. For scenarios C1, C3, and C4, the 2001 Arequipa (Peru) STF (Fig. 5c) was used (Caldeira 2004). In scenario C2, which corresponds to a bilateral rupture, the STF represented in Fig. 5d was used. Except for scenarios S6 and C2, which represent bilateral ruptures, all of the scenarios are unilateral. The ruptures defined in scenarios S1, S2, S3, S4 C1,

Table 1 Rupture parameters used to calculate the synthetic seismograms

Scenario	Fault geometry		Subevents			Rupture definition		Observation distance
			Rake	Distance	Time separation	Direction	Velocity	
	ϕ (deg)	δ (deg)	λ (deg)	ΔD (km)	Δt (s)	λ_r (deg)	v_r (km/s)	Δ (deg)
S1 U	67.5	45.0	80.0	2.6	1.0	0.0	2.60	30
S2 U	7.5	45.0	-80.0	2.6	1.0	0.0	2.60	30
S3 U	7.5	90.0	0.0	2.5	1.0	0.0	2.50	30
S4 U	67.5	45.0	80.0	2.6	1.0	0.0	2.60	Vary
S5 U	52.5	45.0	80.0	2.8	1.0	-30.0		
S6 B	67.5	45.0	80.0	3.5	1.0	0.0 ^a	2.80	Vary
						180.0 ^b	3.55	30
C1 U	312.0	13.0	60.0	11.2	4.0	180.0 ^c	2.8	35
C2 B/U	312.0	13.0	60.0	8.5	2.5	0 ^d	3.4	35
C3 U	312.0	13.0	60.0	10.8	4.0	180.0	2.7	Vary
C4 U	312.0	13.0	60.0	5.08	5.08	180.0	1.0	Vary

U unilateral, B bilateral

^aFirst part of the rupture

^bSecond part of rupture

^cBilateral in the first 15 s, with simultaneously 0° and 180°

^dUnilateral in strike direction

C2, C3, and C4 correspond to horizontal ruptures on a fault plane with different source mechanisms or rupture velocity (Table 1); scenario S5 corresponds to an oblique rupture ($\lambda_r = 30^\circ$) and, therefore, contains a vertical component. In the simple bilateral scenario S6, the rupture spreads in the azimuth direction in the first 10 s and subsequently moves in the reverse direction; in both cases, it has a velocity of 3.55 km/s. However, in the complex bilateral scenario, C2, the rupture was defined with more realistic behavior: In the first 15 s, it spreads simultaneously in two opposite directions (132° and 312°), with each controlled by a temporal function, which is represented in

Fig. 5d. In the last part of the rupture (between 17.5 and 35 s), the spread continues only in the 312° direction (Table 1).

For each scenario, P vertical waveforms were produced at a set of observation points distributed around the epicenter. In scenarios S1, S2, S3, S6, C1, and C2, all of the synthetic seismograms were computed at the same epicentral distances and uniformly distributed (with an interval of 15°) around the source. In scenarios S4, S5, C3, and C4, variable distances were considered: For S4 and S5, distances between 30° and 90° were used but were uniformly distributed around the source; for C3 and C4, a real distribution of seismic stations—the

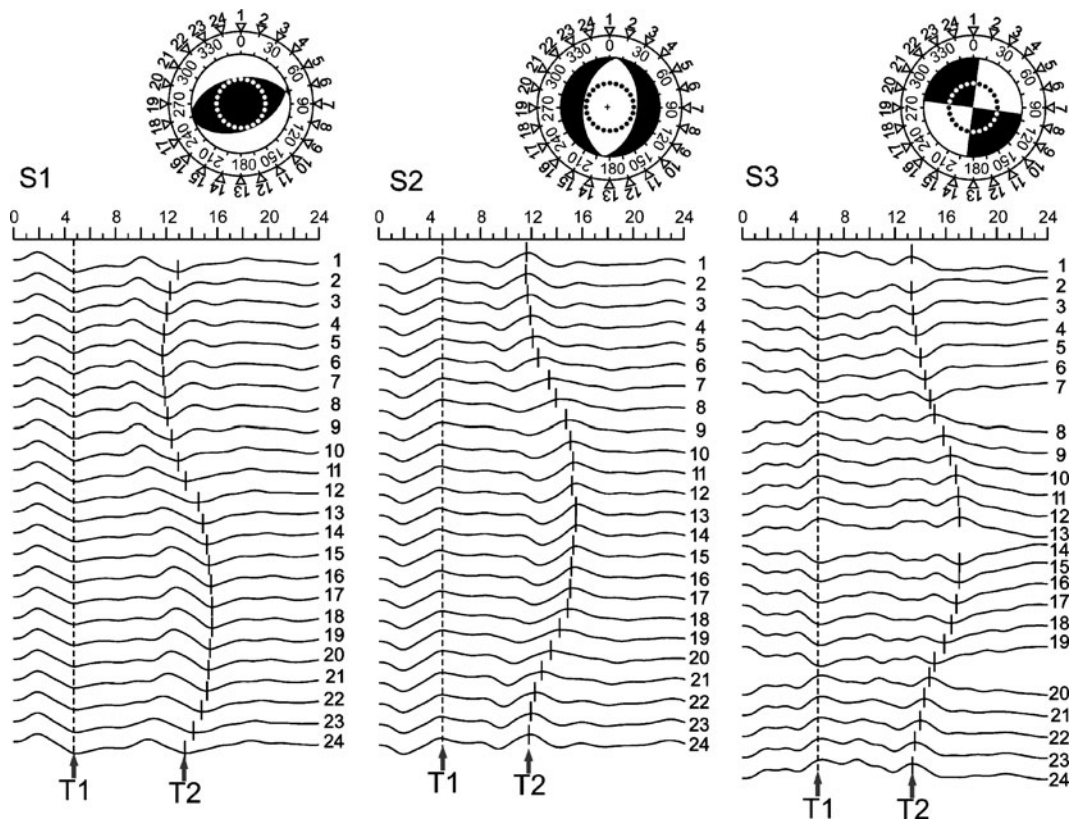


Fig. 6 Synthetic seismograms modeled for simple scenarios (S1, S2, and S3) generated with STF represented in Fig. 5a with normalized amplitudes. The seismograms are azimuthally aligned, and the code number of each receiver point is shown on the right. The receiver positions are marked in the top schemes by numbered inverted triangles on the angular scale and, in the focal sphere, by small open circles. The chosen common pulses are marked by a dashed line (T1) and vertical lines (T2). In S1, for the

observation distance used (30°), all the receiver points are within compressive regions. As a result, the phase inversion effect due to the radiation pattern is not incorporated. This also occurs with scenario S2 relative to the dilatation regions. Scenario S3 corresponds to a strike-slip mechanism in which the crossed nodal zones produce an inversion of the phase polarity observed in the seismograms. For more details, see the text and Tables 1, 2, and 8

case study of the Arequipa (Peru) earthquake—was considered. Figures 6, 7, 8, and 9 represent the waveforms for each scenario, where the chosen common pulses are marked as T1, T2,... (the time intervals between these pulses are provided in the “Appendix”, Tables 8 and 9).

3.2 Results

The results of applying DIRDOP to the synthetic data are represented in Figs. 10, 11, 12, and 13. For the scenarios in which the observation points are equidistant from the source (scenarios S1, S2, S3, S6, C1, and C2), the read delays coincide with the normalized ones. In the other four scenarios (S4, S5, C3, and C4), because the stations are located

at different distances from the source, the delays needed to be normalized to a standard distance.

For all scenarios, the curve of the model (adjusted delays) was calculated from the rupture parameters (velocity, v_r , and azimuth γ), which were obtained from $\Delta\tau^*$ by least squares fitting (Menke 1984). Table 2 and Figs. 10, 11, 12, and 13 summarize the results for each scenario.

3.3 Simple scenarios

For the simple scenarios in which the rupture velocity is defined only by a horizontal component (S1, S2, S3, S4, and S6), the estimated values of γ and v_{rH} correspond precisely to the fault azimuth φ and rupture velocity v_r (Table 2). The

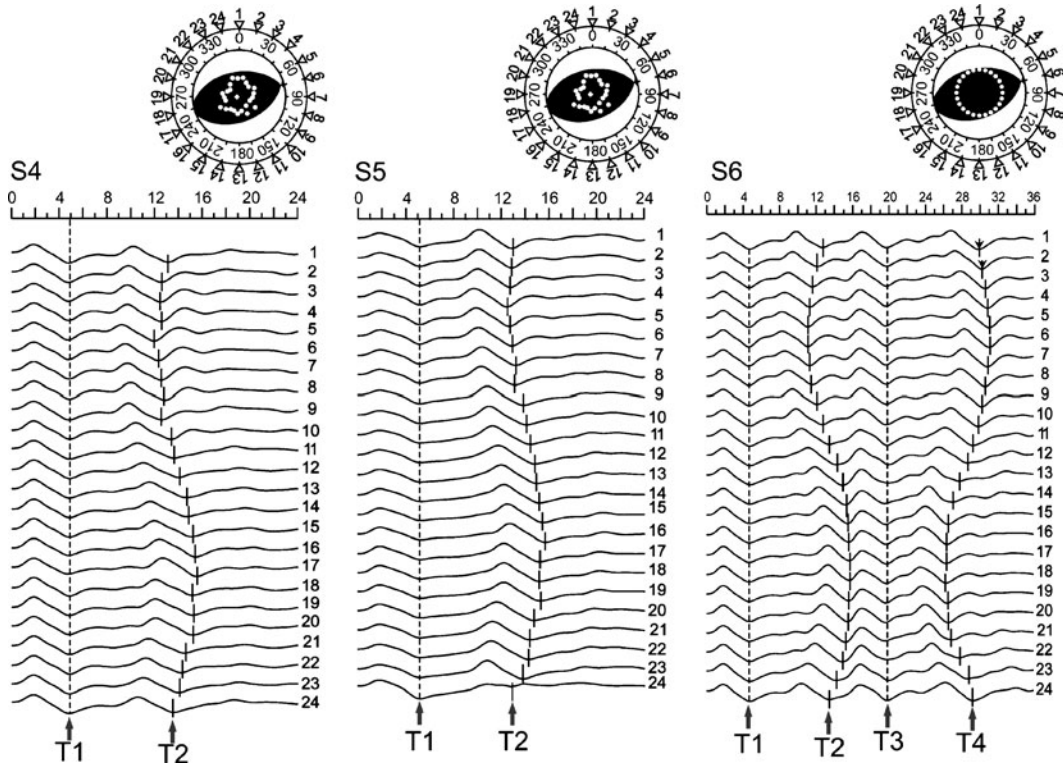


Fig. 7 Synthetic seismograms with a normalized amplitude relative to simple scenarios S4, S5, and S6 generated with STF represented in Fig. 5a, b. The seismograms are azimuthally aligned, and the code number of each receiver point is shown on the right. The receiver positions are marked in the top schemes by numbered inverted triangles on the angular scale and, in the focal sphere, by small open circles. The selected common pulses are marked by

a dashed line (T1) and vertical lines (T2, T3, and T4). Scenarios S4 and S5 describe unilateral extended ruptures with observation sites at variable distances (between 30° and 90°). S4 describes a horizontal rupture and S5 an oblique rupture. S6 is a bilateral rupture, in which two steps are distinguished (T1–T2 and T3–T4). For more details, see the text and Tables 1, 2, and 8

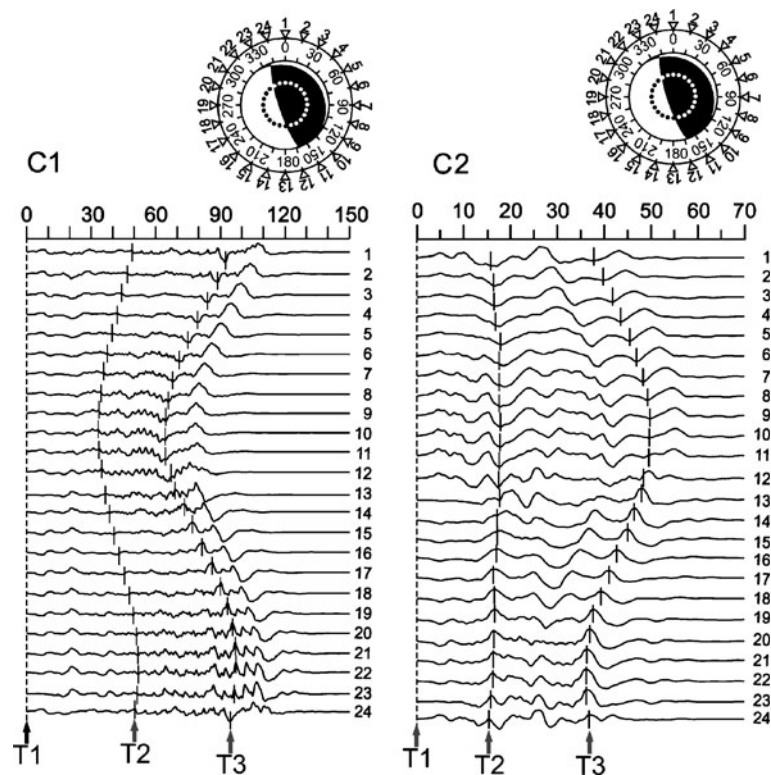


Fig. 8 Synthetic seismograms, with the amplitude normalized relative to complex scenarios C1 and C2, generated with a complex STF represented in Fig. 5c, d, respectively. The seismograms are azimuthally aligned, and the code number of each receiver point is shown on the right. The receiver positions are marked in the top schemes by numbered inverted triangles on the angular scale and, in the

focal sphere, by *small open circles*. The selected common pulses are marked by a *dashed line* (T1) and *vertical lines* (T2, T3). Scenario C1 describes a unilateral rupture and C2 a bilateral rupture with observation sites at a fixed distance of 35° . For the two scenarios, two steps are distinguished (T1–T2 and T2–T3). For more details, see the text and Tables 1, 2, and 8

results obtained by DIRDOP and the parameters used to compute the synthetic seismograms are in agreement. Concerning the rupture azimuth, the actual results show a better correlation with the expected ones than the error estimates would suggest (Table 2). Relative to the estimates of rupture velocity, the results are globally within the margin of error, except in S4, where we obtained a value that exceeded expectations by about 8% (in this case, the margin of error is 7%). The calculation of rupture velocity because it is more complex (nonlinear inversion) is more sensitive to the parameters of the procedure and consequently more prone to errors.

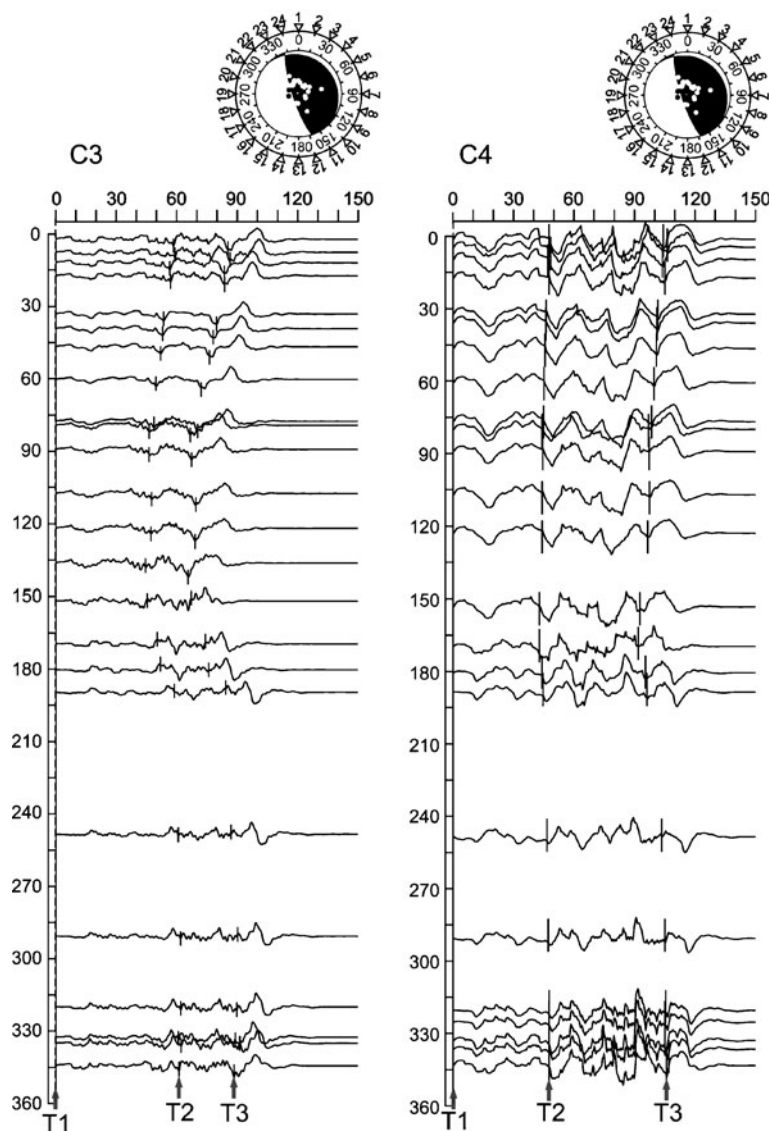
Scenarios S1, S2, and S3 were used to test the sensitivity of different focal mechanisms. For this, we simulated similar horizontal ruptures but em-

ployed different focal mechanisms (reverse, normal, and strike-slip). The results prove that this approach is insensitive to the focal mechanism.

The identification of common pulses on teleseismic data from dip-slip events is simplified. As adjacent azimuthal stations maintain polarity, the general aspects of seismograms are preserved, and as a consequence, recognizing common pulses is simpler. For strike-slip or oblique mechanisms, identification may become more difficult. The shape of the seismic trace completely changes when the nodal zones are crossed; this fact can complicate the identification of common pulses. This effect is visible in scenario S3 (Fig. 6).

In scenario S5, we wanted to test the influence of the vertical component of the rupture velocity on the inversion results and, consequently, ana-

Fig. 9 Synthetic seismograms with a normalized amplitude, relative to complex scenarios C3 and C4 generated with STF represented in Fig. 5c. The seismograms are azimuthally aligned according the positions listed in Table 9. The chosen common pulses are marked by aligned to initial time line (T1) and vertical lines (T2, T3). Scenario C3 allows us to test the sensitivity of the method relative to a poor coverage of stations. In this case, we have used a rupture process, similar to that described in C1, but with a realistic station distribution that presents a gap of 60°. Scenario C4 tests the ability of the method to resolve low rupture velocities. For the two scenarios, two steps are distinguished (T1–T2 and T2–T3). For more details, see the text and Tables 1, 2, and 9



lyze the ability of the method to estimate this component of the rupture velocity. DIRDOP finds only the horizontal component of the rupture velocity vector v_{rH} and its errors (Fig. 4). However, if the azimuth and dip of the fault are known (determined by independent methods), v_r can be calculated within the allowed limits by the estimated errors of v_{rH} (Fig. 4). In this case, the v_r and the plunge angle (λ_r) obtained, respectively, from Eqs. 10 and 11 are $v_r = 2.7 \pm 0.30$ km/s and $\lambda_r = 29.1 \pm 10^\circ$. These values are in agreement with those used in the rupture modeling represented in Table 1.

Scenario S6 refers to an asymmetric bilateral rupture. The bilateral effects are clearly shown in the synthetic seismograms (Fig. 7), where it is easy to identify two pairs of pulses related to the two stages of the rupture. The high quality of the results obtained for this case (Table 2) indicates the simplicity of the rupture.

3.4 Complex scenarios

For the unilateral rupture scenario C1 with regular coverage, the synthetic seismograms (Fig. 8)

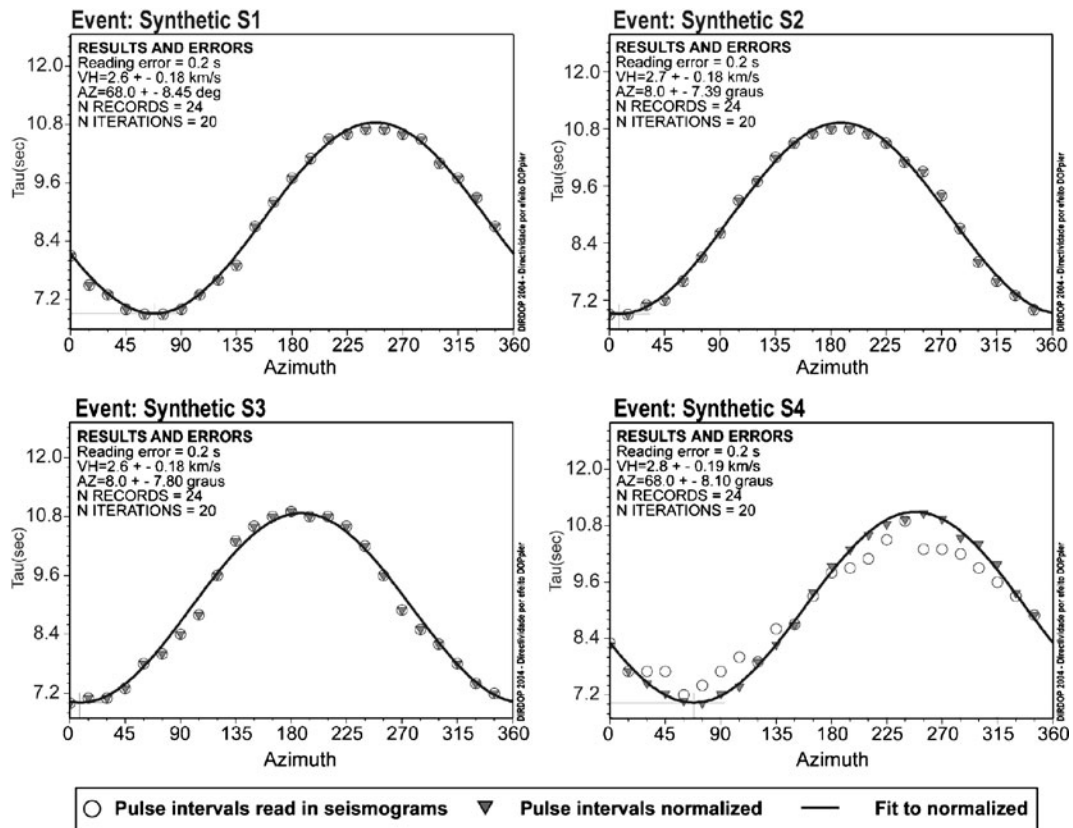


Fig. 10 DIRDOP results for the simple scenarios S1, S2, S3, and S4. Plots of common time-delays versus azimuth of the receiver point. *Open circles* represent the time delays read in the synthetic waveforms of Figs. 6 and 7 and listed in Table 8. *Triangles* represent normalized pulse delays. The curves show the fit of the normalized pulse delays in relation to the parameters of the DIRDOP model. Note that the azimuth of the rupture corresponds to the minimum

of this curve, marked by *AZ*; *VH* is the horizontal rupture velocity and is estimated using Eq. 6. In S1, S2, and S3, all observation points are at the same distance from the epicenter; one consequence of this is a coincidence between the read and normalized time delays. In S4, because the observation sites are at different hypocentral distances, this coincidence does not occur. The corresponding obtained values are listed in Table 8

are more complex when compared with similar ones from the simple situation S1 (Fig. 6). This fact does not increase the difficulty of identifying one or two pairs of common pulses. The estimated rupture velocity is equal to that used to generate the synthetic data; the errors in the rupture direction are of the same order of magnitude as the azimuth's gap (15°).

In the bilateral section of scenario C2 (the first 15 s), we noted a discrepancy between the results and the parameters used in the simulation (Table 2). The estimated velocity (1.0 km/s) is significantly lower than the expected value (3.4 km/s), and the errors associated with the

direction of rupture are very high ($\sim 242^\circ$) when compared with the stations gap. These results can be clearly observed in the wide dispersion of data in the theoretical curve (Fig. 12). To explain this, we suggest that when the rupture progresses simultaneously in more than one direction with equivalent energies, the interferences between the waves coming from different rupture fronts diminish the directive effects in the seismic records. In such scenarios, it is very difficult to identify the required common pulses with the necessary accuracy. This result suggests the failure of the method in cases of bilateral ruptures. Thus, in cases in which similar results are obtained (poor

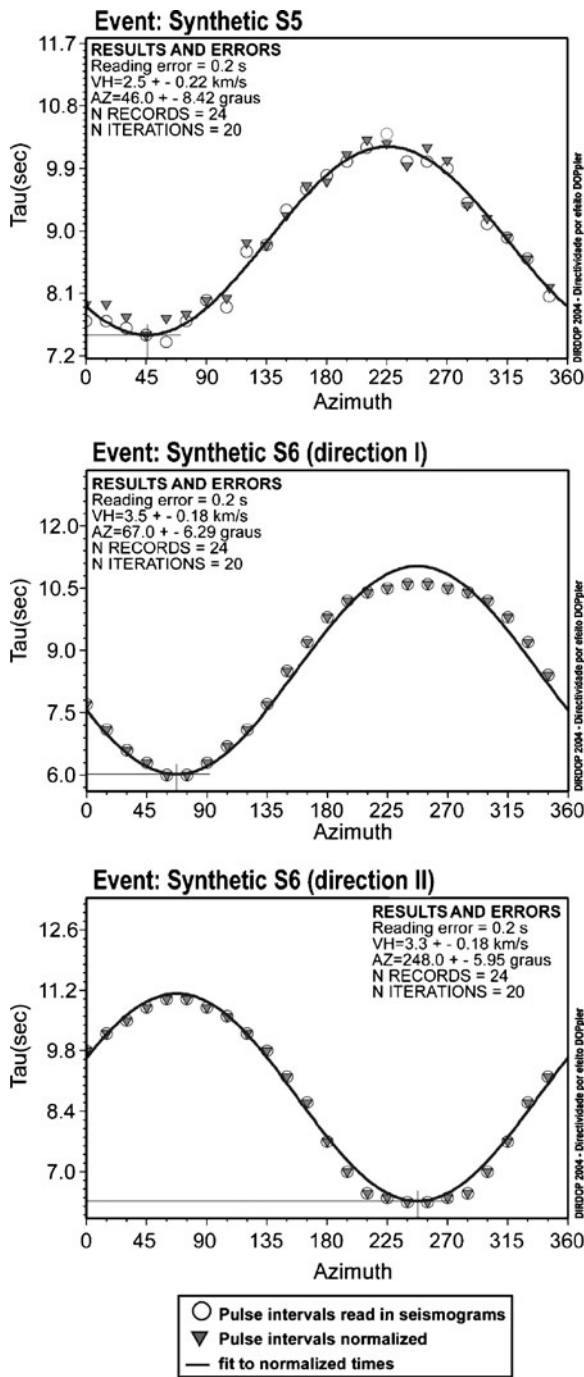


Fig. 11 Results for simple scenarios S5 and S6. Plots of pulse delay as a function of the azimuth of the receiver point. *Open circles* denote the read delays shown in Table 8; *triangles* represent the normalized read delays, and the *curve* shows the fit of the normalized delays to the model. *AZ* denotes the rupture azimuth, which corresponds to the abscissa of the minimum of the curve; *VH* is the rupture velocity calculated from Eq. 6. The corresponding obtained values are listed in Table 8

adjustment of the dataset to the theoretical model, unexpected values for the rupture velocity when compared with other sections of the same rupture, and direction errors much higher than in the station gap), they can be associated with bilateral or circular ruptures. In the last part of the rupture (17.5–35 s), which corresponds to a unidirectional section, the results fit well with the expected values, which allow us to conclude that this approach can also discriminate between sections of the rupture.

Scenario C3 allows us to test the sensitivity of the method relative to poor station coverage. To achieve this, we used a similar rupture scenario as described for C1 but with a realistic station distribution that presents a gap of 60°. As in scenario C1, the results (Fig. 13; Table 2) show consistency with the values used to generate the synthetic data. However, in scenario C3, the errors are larger and, in the direction of the rupture, display an order of magnitude of the gaps between stations.

Finally, scenario C4 tests the ability of the method to resolve low rupture velocities. The synthetic seismograms used (Fig. 9) exhibit the characteristic marks of directivity less obviously than in the other scenarios, but the difficult to identify common pulses do not increase. However, the numerical results and relative errors (Fig. 13; Table 2) show a larger mismatch between the expected values and the corresponding calculated values for the slow rupture.

The most significant conclusion of the tests is that in unilateral cases in which the common pulses are correctly identified, the errors associated with the rupture direction and rupture velocity depend on the angular coverage. We verify that the error associated with the rupture direction is, in general, of the same order of magnitude as the maximum azimuthal gap. For bilateral scenarios, the interference between the radiation arising from opposing sides of the rupture fronts makes the identification of common pulses difficult. As a consequence, the adjustment of the dataset to predictions of the theoretical model is poor and the error level increases. The analysis of the method allows us to conclude that if the gaps coincide with the azimuth of the extrema of Eq. 6, the constraint of this extrema fails, which can affect the estimate obtained for the rupture velocity.

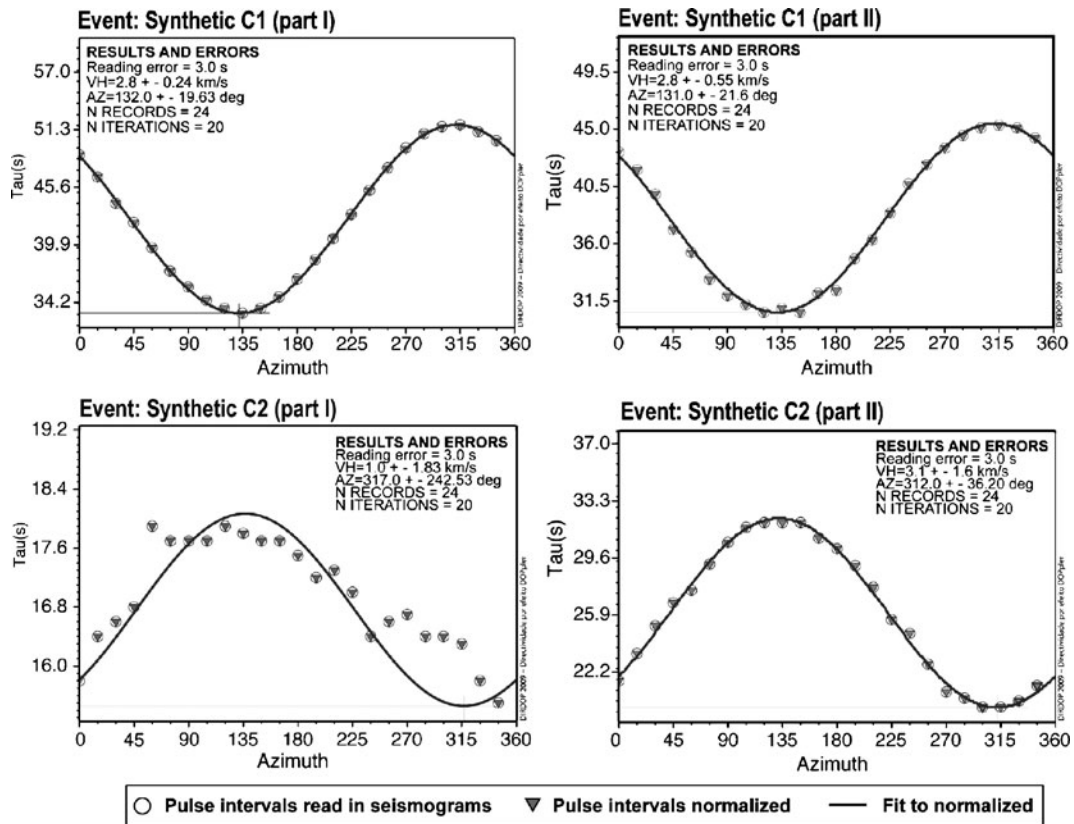


Fig. 12 Results for the complex scenarios C1 and C2. Plots of pulse delay as a function of the azimuth of the receiver point. *Open circles* denote the read delays shown in Table 8; *triangles* represent the normalized read delays, and the *curve* shows the fit of the normalized delays to

the model. *AZ* denotes the rupture azimuth, which corresponds to the abscissa of the minimum of the curve; *VH* is the rupture velocity calculated from Eq. 6. The corresponding values obtained are listed in Table 8

4 Applications to real data

Here, we present four applications of the method to real data; for this, four earthquakes with significant magnitude occurring in the past 10 years were selected (Fig. 14):

1. Arequipa, Peru ($M_w = 8.4$; June 23, 2001)

This event, the first M8 class earthquake in the twenty-first century, related to the convergence between the Nazca and South American plates, occurred near the coastline of southern Peru, in the Arequipa region, about 80 km northwest of Ocoña. The destruction spread over a vast area that included all of southern Peru (maximum intensity of VIII, MM scale) and some parts of northern Chile and Bolivia (Tavera et al. 2002).

According to the US Geological Survey (USGS), the hypocenter was at latitude 16.26° S, longitude 73.64° W, and had a depth of 33.0 km. The Harvard Centroid Moment Tensor (CMT) mechanism solution (Fig. 14) indicates an inverse fault plane trending toward the NW with shallow dipping (strike = 318° ; dip = 14° ; rake = 79°). The spatiotemporal slip estimated by body wave inversion points to a unilateral rupture that propagated from NW to SE on a fault plane with an area of $180 \times 100 \text{ km}^2$ (Bilek and Ruff 2002).

2. Denali, AK, USA ($M_w = 7.8$; November 3, 2002)

Most of the seismic activity in Alaska results from the interaction of the northwestward-moving Pacific plate with the corner of the North

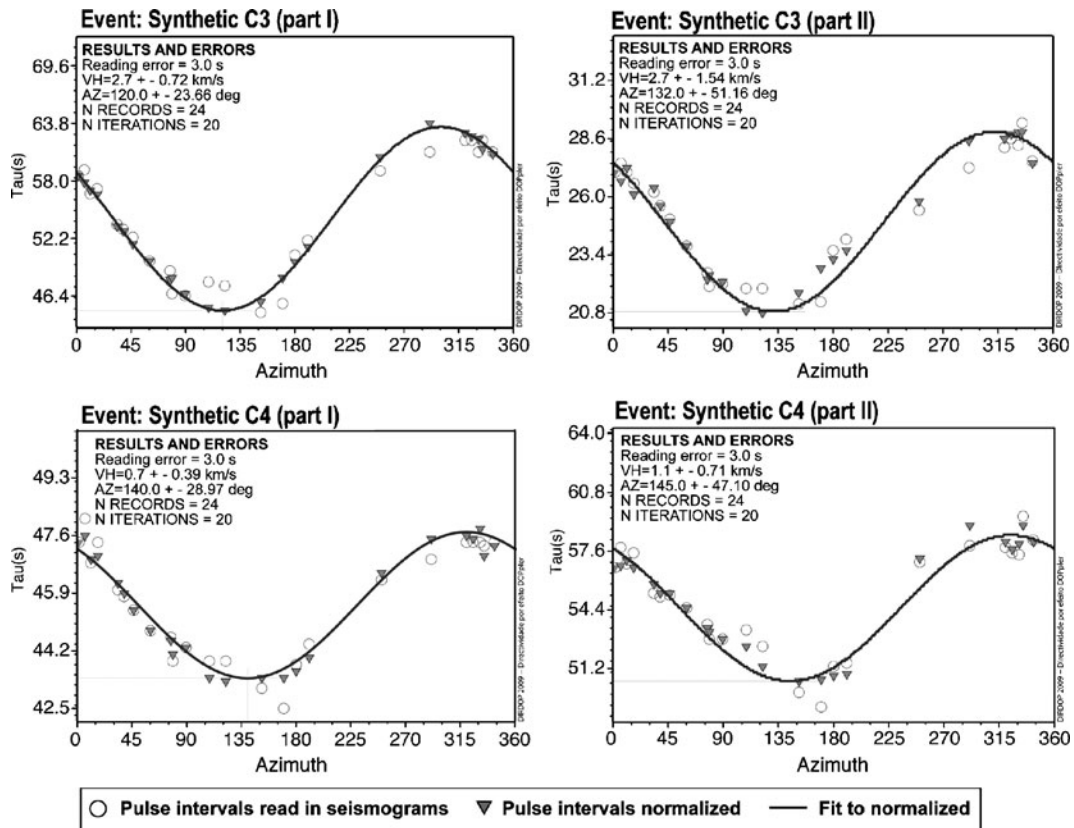


Fig. 13 Results for the complex scenarios C3 and C4. Plots of pulse delay as a function of the azimuth of the receiver point. *Open circles* denote the read delays shown in Table 9; *triangles* represent the normalized read delays, and the *curve* shows the fit of the normalized delays to

the model. *AZ* denotes the rupture azimuth, which corresponds to the abscissa of the minimum of the curve; *VH* is the rupture velocity calculated from Eq. 6. The corresponding values obtained are listed in Table 9

American plate that comprises Alaska. This event (Fig. 14) ruptured three different faults ending on November 3, 2002, with a total surface rupture length of ~340 km, consistent with the right-lateral strike-slip focal mechanism (Eberhart-Phillips et al. 2003). The rupture started as a thrust event (Eberhart-Phillips et al. 2003) onto the main strand of the Denali–Totschunda fault system and continued as a right-lateral strike-slip event for ~220 km until it reached the Totschunda fault near 143° W longitude. At that point, it right-stepped onto the more southeasterly trending Totschunda fault and stopped after rupturing nearly 70 km of the fault. This event caused significant damage to the Trans-Alaska Pipeline, and multiple landslides and rock avalanches occurred in the Alaska Range, with the largest slide

on the Black Rapids Glacier. According to the USGS, the hypocenter was at latitude 63.520° N, longitude 147.530° W, and had a depth of 5.0 km. The Harvard CMT mechanism solution (Fig. 14) indicates a NW rupture plane (strike = 296°; dip = 71°; rake = 171°). The source model, estimated by body wave inversion, points to a unilateral rupture that propagated from NW to SE on a fault plane with an area of 340 × 15 km² (Ozacar and Beck 2004).

3. Zemmouri–Boumerdes, Algeria (*M_w* = 6.8; May 21, 2003)

This 2003 earthquake (Fig. 14), which was generated by a submarine fault, occurred at the boundary region between the Eurasian and African plates. From a geodynamic point of view, the

Table 2 Directivity parameters obtained for synthetic tests

Scenario	Direction and rupture velocity used in the rupture modeling		Direction and rupture velocity obtained by method application	
	ϕ^a (deg)	v_r^a (km/s)	$\gamma \pm \Delta\gamma^a$ (deg)	$v_{rH} \pm \Delta v_{rH}^a$ (km/s)
S1	67.5	2.60	68.0 ± 8.45	2.6 ± 0.18
S2	7.5	2.60	8.0 ± 7.39	2.7 ± 0.18
S3	7.5	2.50	8.0 ± 7.80	2.6 ± 0.18
S4	67.5	2.60	68.0 ± 8.10	2.8 ± 0.19
S5	52.5	2.80	46.0 ± 8.42	2.5 ± 0.22
S6 (bilateral)	67.5 ^b	3.55	67.0 ± 6.20^b	3.5 ± 0.18
	247.5 ^c		248.0 ± 5.95^c	3.3 ± 0.18
C1	132.0	2.8	132.0 ± 19.63	2.8 ± 0.18
			131.0 ± 21.60	2.8 ± 0.55
C2	312.0 and ^d 132.0 312 ^e	3.4	317.0 ± 242.53	1.0 ± 1.83
			312.0 ± 36.20	3.1 ± 1.6
C3	132.0	2.7	120.0 ± 23.66	2.7 ± 0.72
			132.0 ± 51.16	2.7 ± 1.54
C4	132.0	1.0	140.0 ± 28.97	0.7 ± 0.39
			145.0 ± 47.10	1.1 ± 0.71

^aExcept for S5, the fault azimuth (ϕ) coincides with the horizontal rupture direction (γ) and v_r coincides with v_{rH}

^bFirst step of rupture

^cSecond step of rupture

^dBilateral part between 0 and 15 s

^eUnilateral part between 15 and 35 s

Mediterranean basin shows a collision process between these two tectonic plates in the NW–SE direction. The shortening rate, estimated previously for the 2003 event, is about 2.5 mm/year (Bufoin et al. 2004). These relative plate motions create a compressional tectonic environment with mostly thrust-faulting and strike-slip fault-

ing mechanisms (Bezzeghoud and Bufoin 1999). The Tellian Atlas (the major geological feature in northern Algeria) is characterized by reverse faults trending in a NE–SW direction; other types of faults, such as normal and strike-slip faults, are present in different seismogenic zones of northern Algeria (Bezzeghoud and Bufoin 1999).

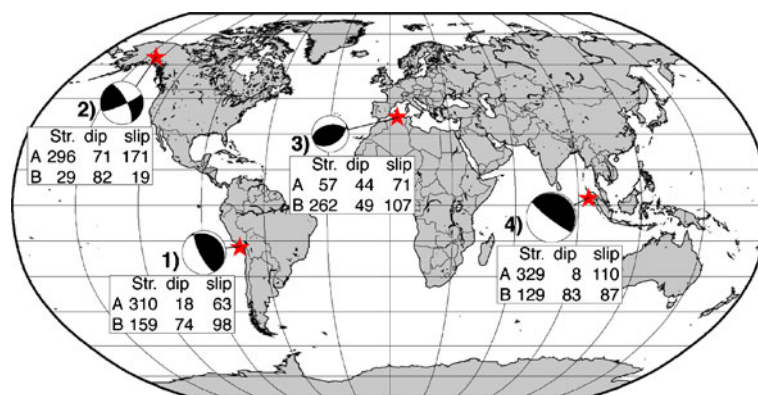


Fig. 14 Map of the studied earthquakes: 1 Arequipa, Peru ($M_w = 8.4$; June 23, 2001); 2 Denali, AK, USA ($M_w = 7.8$; November 3, 2002); 3 Zemmouri–Boumerdes, Algeria

($M_w = 6.8$; May 21, 2003); 4 Sumatra, Indonesia ($M_w = 9.3$; December 26, 2004). Main shock focal mechanisms are taken from the Harvard CMT catalog

This $M_w = 6.8$ event was located offshore at 37.02° N and 3.77° E and a focal depth of 7 km in a zone characterized by relatively moderate and diffuse seismicity (Ayadi et al. 2003). The main shock has been relocated using HypoDD (Ayadi et al. 2008) at Zemmouri el Bahri village, close to the continent, at 36.83° N and 3.65° E. This earthquake is the second largest to occur in Algeria since the 1980 El Asnam $M_s = 7.3$ earthquake. In the epicentral area, the main shock severely affected the towns and villages, particularly the coastal towns of Zemmouri and Boumerdes. The earthquake killed 2,271 people, injured 11,455 (official toll), and caused great damage, mainly to the cities of Boumerdes, Algiers, and Dellys. The Harvard CMT mechanism solution (Fig. 14) indicates an ENE–WSW rupture plane (strike = 57° ; dip = 44° ; rake = 71°). The source model, estimated by joint inversion of body wave and teleseismic data, points to a bilateral rupture that propagated from the hypocenter on a fault plane with an area of $60 \times 24 \text{ km}^2$ (Delouis et al. 2004).

4. Sumatra, Indonesia (the strongest earthquake; $M_w = 9.3$; December 26, 2004)

This megathrust-faulting earthquake ($M_w = 9.3$) occurred at the interface of the India and Burma plates along the Sunda Trench fault line and was caused by the release of stresses that developed as the India plate subducted beneath the overriding Burma plates. The two plates are converging (dextral–oblique convergence) at a rate of 6 cm/year (Tregoning et al. 1994), and the complex tectonics of the region involve several plates, including the Australia, Sunda, Eurasia, India, and Burma plates (i.e., Bilham et al. 2005). Due to this elevated convergence rate, the region in which both earthquakes occurred is one of the world’s most seismically active regions. This earthquake triggered a massive tsunami that affected several countries throughout South and Southeast Asia, including Indonesia, Sri Lanka, India, Thailand, Somalia, Myanmar, Malaysia, Maldives, Tanzania, and Bangladesh. The tsunami crossed into the Pacific Ocean and was recorded along

Table 3 Phases Peru

Station name	Azimuth (deg)	Δ (deg)	Time of common pulses used (s)		
			T1	T2	T3
HRV	1.51	58.67	0.00	51.45	96.12
SDV	6.24	25.16	0.00	51.03	96.14
DRLN	11.15	66.88	0.00	47.45	92.83
FDF	16.81	32.17	0.00	45.07	92.65
DSB	33.40	89.86	0.00	44.76	86.20
CMLA	38.51	70.12	0.00	44.28	84.95
PAB	46.26	89.90	0.00	44.07	83.56
SACV	60.21	58.10	0.00	39.88	74.17
DBIC	77.02	71.45	0.00	38.80	72.34
RCBR	78.58	38.07	0.00	38.31	71.19
ASCN	89.36	58.06	0.00	36.96	70.54
TSUM	108.72	85.56	0.00	38.63	70.02
SUR	122.24	84.80	0.00	39.19	69.69
HOPE	151.71	47.57	0.00	38.49	65.75
NIEB	169.82	20.26	0.00	40.29	65.73
SPA	180.00	73.86	0.00	42.95	74.18
SBA	190.67	80.16	0.00	42.10	77.29
RAR	250.41	80.97	0.00	51.85	91.34
POHA	291.14	88.35	0.00	53.17	94.81
PAS	320.27	65.96	0.00	55.32	96.62
WUAZ	325.82	62.70	0.00	54.09	97.42
NEW	331.54	75.28	0.00	52.85	97.30
HKT	334.70	50.96	0.00	54.84	99.25
CCM	343.14	56.75	0.00	52.82	98.64

Distribution of the seismic stations and measured time of common pulses for the Arequipa, Peru earthquake ($M_w = 8.4$; June 23, 2001)

the west coast of South and North America. The Harvard CMT mechanism (Fig. 14) revealed a SSE–NNW rupture plane (strike = 329°; dip = 8°; rake = 110°). Using data collected by the German Regional Seismic Network and applying array techniques, Krüger and Ohrnberger (2005a, b) find a total rupture length of 1,150 km. From the epicenter (3.316° N, 95.854° E, USGS), the rupture extended 1,200–1,300 km along the Sunda Trench toward the north–northwest (Ammon et al. 2005; Ni et al. 2005; Vigny et al. 2005) with a downdip width of ~200 km (Ammon et al. 2005).

4.1 Data

The most delicate and painstaking step involved in applying the method to real data is identifying

common pulses in all seismograms. Given a set of seismograms that record an earthquake at several stations around the source, it is often difficult to recognize common seismic pulses. This difficulty is due mainly to a combination of three factors: (a) interference with phases of other subevents that could mask the sought-after pulse, (b) pulse shifts due to differences in the epicentral distance, and (c) the influence of the radiation pattern. Therefore, this step requires the selection of criteria based on practical experience with seismogram analyses. A good azimuth distribution of high quality waveforms is the first requirement. After being azimuthally ordered and aligned by the time of arrival of the P wave, the waveforms must reveal some common pulses that can be followed on almost all of the seismograms. When a particular phase is followed across a set of seis-

Table 4 Phases Alaska

Station name	Azimuth (deg)	Δ (deg)	Time of common pulses used (s)		
			T1	T2	T3
TRTE	3.47	58.13	0.00	6.20	61.89
RUE	12.58	63.22	0.00	6.30	60.40
KONO	13.73	55.72	0.00	6.30	60.20
CART	26.77	75.60	0.00	6.60	58.90
MTE	31.07	71.49	0.00	6.80	58.20
SFJ	40.77	36.67	0.00	6.40	54.50
DRLN	62.72	47.49	0.00	6.80	49.60
LBNH	77.78	45.47	0.00	6.70	45.90
BBSR	80.24	58.46	0.00	6.70	47.10
PAL	82.06	47.20	0.00	7.00	46.00
MYNC	95.65	47.56	0.00	6.30	43.70
CCM	100.15	41.94	0.00	6.50	43.20
WMOK	110.54	41.51	0.00	6.30	42.90
TX32	119.66	44.29	0.00	6.20	44.00
SDD	133.95	35.48	0.00	5.80	44.70
SBC	136.14	34.02	0.00	5.80	44.90
PTCN	164.09	89.60	0.00	6.30	54.00
POHA	190.61	44.28	0.00	5.50	56.90
KIP	194.21	42.87	0.00	5.00	57.20
MIDW	222.47	40.34	0.00	6.70	63.80
KWAJ	231.07	63.34	0.00	6.40	63.10
WAKE	236.61	54.01	0.00	6.40	64.70
PMG	243.65	87.77	0.00	6.00	63.10
MAJO	274.88	51.02	0.00	5.10	70.10
MDJ	288.01	48.15	0.00	5.60	70.10
BJT	295.15	57.52	0.00	5.80	68.20
KURK	328.04	60.26	0.00	6.00	66.90
CHK	334.57	59.19	0.00	5.80	66.50
ANTO	359.62	76.73	0.00	5.90	61.60

Distribution of the seismic stations and measured time of common pulses for the Denali, AK, USA earthquake ($M_w = 7.8$; November 3, 2002)

mograms, its shape changes. The level of these variations is such that, in some cases, we can even note polarity inversions, in particular when nodal zones are crossed. Sometimes, the identification of “difficult pulses” must be facilitated through the use of theoretical travel times and the radiation pattern.

For the four applications described previously, we used teleseismic broadband vertical waveforms supplied by the Incorporated Research Institutions for Seismology Data Management Center consortium. The selected stations are located at distances between 30° and 90° from the epicenter. Tables 3, 4, 5, and 6 provide complete information regarding the stations used (name, azimuth, and epicentral distance), as well as the

time of common pulses used in the inversion for each seismic event:

1. Arequipa, Peru ($M_w = 8.4$; June 23, 2001)

For the Arequipa directivity study, data from 24 stations span an azimuthal coverage with an average angular interval of 15° and a major gap of 59.74° southwest of the epicenter, between stations SBA and RAR (Table 3). In the selected waveforms represented in Fig. 15, we applied the above criteria and identified three common pulses indicated by T1, T2, and T3. The seismograms after the last phase identified (~82 s) become too complex to permit clear identification of other common pulses. Reading errors in the seismograms of 1.5 s were assumed.

Table 5 Phases Algeria

Station name	Azimuth (deg)	Δ (deg)	Time of common pulses used (s)		
			T1	T2	T3
KBS	2.34	42.28	0.0	4.8	11.8
BILL	6.67	74.55	0.0	5.5	11.4
MA2	16.35	80.07	0.0	4.6	11.4
YSS	26.72	88.79	0.0	4.7	11.6
HIA	37.16	77.19	0.0	4.4	11.8
TLY	41.59	67.53	0.0	4.3	13.2
BJT	45.89	81.47	0.0	4.4	13.1
CHK	47.31	48.08	0.0	4.1	13.6
ENH	56.94	83.57	0.0	4.2	13.6
AAK	60.42	53.22	0.0	4.1	13.9
QIZ	65.40	90.92	0.0	4.4	13.3
LSA	66.87	70.93	0.0	4.1	13.7
KMBO	133.00	48.93	0.0	4.3	13.1
MBAR	140.05	44.90	0.0	4.4	13.2
LSZ	151.52	56.77	0.0	4.6	12.2
LBTB	158.14	64.92	0.0	4.7	12.0
SUR	164.78	70.73	0.0	4.9	11.8
DBIC	196.79	31.10	0.0	4.9	10.7
RCBR	229.71	56.39	0.0	5.8	10.2
LPAZ	246.30	85.73	0.0	5.8	10.5
SAML	248.67	77.43	0.0	5.8	10.6
OTAV	265.53	83.64	0.0	5.9	10.1
BBSR	287.06	55.43	0.0	5.8	10.8
GOGA	296.43	68.91	0.0	5.7	11.3
DRLN	306.00	45.26	0.0	5.5	10.9
ANMO	309.13	83.51	0.0	5.6	11.1
BOZ	319.86	79.36	0.0	5.3	11.1
FRB	326.38	49.94	0.0	5.9	11.6
INK	344.47	70.38	0.0	5.1	11.6
COLA	347.94	76.15	0.0	5.1	11.8

Distribution of the seismic stations and measured time of common pulses for the Zemmouri–Boumerdes, Algeria earthquake ($M_w = 6.8$; May 21, 2003)

Table 6 Phases Sumatra

Station name	Azimuth (deg)	Δ (deg)	Time of common pulses used (s)				
			T1	T2	T3	T4	T5
TLY	6.35	48.65	0.00	31.64	90.71	174.69	220.74
TIXI	10.46	71.35	0.00	31.53	90.67	175.03	222.71
CHTO	10.56	15.68	0.00	29.48	85.98	170.73	216.15
KMI	16.08	22.66	0.00	31.98	90.81	177.01	223.43
XAN	20.04	32.88	0.00	32.50	92.16	179.02	224.95
BJT	23.02	40.87	0.00	33.13	92.14	179.66	227.54
MDJ	30.74	50.67	0.00	34.26	92.47	178.67	228.24
YSS	35.16	59.34	0.00	33.97	95.05	181.40	231.59
QIZ	39.89	20.69	0.00	34.09	94.13	186.29	237.15
KMNB	43.73	30.16	0.00	34.25	95.44	184.62	240.42
SSLB	47.61	31.58	0.00	33.96	99.74	188.58	243.80
TPUB	48.02	31.05	0.00	34.81	100.08	189.26	245.29
YULB	48.57	31.60	0.00	34.34	99.74	188.92	244.62
TWGB	49.25	31.11	0.00	33.89	97.79	188.22	243.99
GUMO	75.02	49.53	0.00	37.30	103.75	200.56	260.75
DAV	81.55	29.71	0.00	36.27	102.70	200.83	263.71
HNR	101.93	64.97	0.00	39.17	106.23	204.51	266.32
PMG	104.36	52.73	0.00	39.47	109.48	209.00	271.51
CTAO	117.43	54.53	0.00	38.97	109.73	210.23	274.83
EIDS	121.52	60.50	0.00	39.32	110.36	208.82	274.80
WRAB	123.08	44.19	0.00	38.96	110.02	209.81	274.12
ARMA	126.66	62.75	0.00	39.41	110.03	209.32	270.05
STKA	132.58	55.66	0.00	39.89	110.24	209.76	273.33
TOO	136.45	61.29	0.00	38.72	106.72	205.26	271.94
MBWA	136.70	33.65	0.00	39.82	111.34	211.68	275.53
TAU	140.80	65.20	0.00	39.23	109.40	207.15	270.37
KMBL	146.34	42.38	0.00	39.54	108.69	209.69	275.28
BLDU	151.07	39.10	0.00	40.69	110.02	210.14	276.52
NWAO	152.47	41.27	0.00	40.34	109.66	208.03	273.72
DRV	163.46	76.49	0.00	38.16	106.08	201.46	261.80
SBA	168.46	89.21	0.00	36.38	103.16	196.38	256.94
CASY	173.80	70.20	0.00	38.10	105.04	199.55	262.21
AIS	200.99	44.31	0.00	37.63	98.77	187.95	250.01
SUR	236.35	79.29	0.00	35.48	94.80	178.34	235.44
BOSA	239.33	74.78	0.00	35.47	95.46	177.34	235.36
LBTB	242.91	73.74	0.00	35.18	94.80	176.02	232.38
DGAR	245.57	25.78	0.00	34.78	89.81	173.02	229.96
LSZ	252.47	69.56	0.00	34.34	94.12	173.68	228.30
KMBO	266.71	58.87	0.00	33.48	90.24	171.09	218.50
MBAR	267.84	65.33	0.00	34.78	91.68	173.35	220.43
FURI	278.42	57.19	0.00	34.78	88.81	167.52	215.46
TAM	292.64	89.16	0.00	33.56	90.03	173.31	225.97
RAYN	297.13	52.71	0.00	31.11	85.20	162.84	208.45
EIL	301.12	63.32	0.00	32.14	88.42	166.53	214.23
TIP	309.15	79.57	0.00	31.70	87.51	167.56	216.47
ANTO	311.96	67.48	0.00	32.11	87.82	169.40	217.77
GNI	315.76	58.95	0.00	31.78	87.14	167.09	211.84
TIRR	315.82	71.78	0.00	32.01	87.82	167.71	218.11
PSZ	318.17	78.25	0.00	32.59	88.30	169.39	215.48
SUW	324.69	77.27	0.00	32.12	87.81	167.04	213.46
OBN	328.29	70.21	0.00	31.87	87.81	166.38	213.52
VSU	329.63	76.44	0.00	32.22	89.06	168.63	216.66

Table 6 (continued)

	Station name	Azimuth (deg)	Δ (deg)	Time of common pulses used (s)				
				T1	T2	T3	T4	T5
Distribution of the seismic stations and measured time of common pulses for the Sumatra, Indonesia giant earthquake ($M_w = 9.3$; December 26, 2004)	AKTK	331.96	56.82	0.00	31.61	86.50	163.41	207.84
	KZA	337.20	42.84	0.00	31.14	86.17	165.27	211.49
	ARU	337.25	60.79	0.00	31.68	87.21	164.56	208.54
	MKAR	346.87	44.88	0.00	32.12	86.84	163.30	210.90
	LSA	350.60	26.66	0.00	31.80	87.83	166.51	210.24
	WMQ	350.85	41.02	0.00	31.29	88.11	167.36	211.81

2. Alaska, USA ($M_w = 7.8$; November 3, 2002)

This situation involved 29 seismograms spanning an azimuthal coverage with an average angular interval of 13° ; however, a major gap of 33° north–northwest of the epicenter is present be-

tween stations BJT and KURK (Table 4). In the selected waveforms represented in Fig. 16, we applied the above criteria and identified two common pulses indicated by T1 and T2. It is not possible to identify pulses that are more advanced than T2 (~ 60 s). These pulses were considered to have a reading error of 2.0 s.

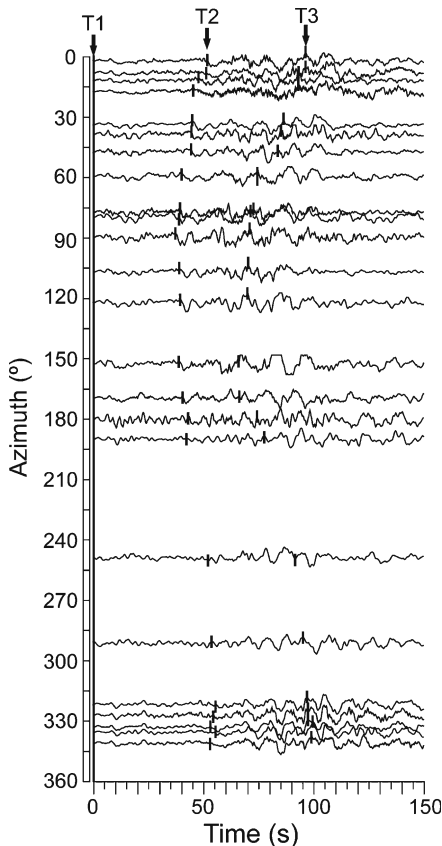


Fig. 15 Vertical P waveforms from the 2001 Arequipa (Peru) earthquake sorted by source-to-station azimuth and aligned at the first-arrived phase (*hatched line*). The three common pulses (T1, T2, and T3) employed in the directivity method are identified by *vertical lines* in each seismogram and are listed in Table 3

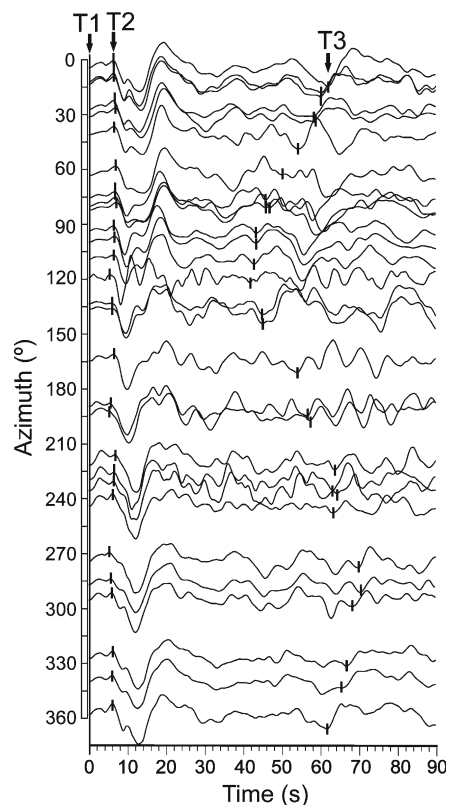


Fig. 16 Vertical P waveforms from the 2002 Denali (AK, USA) earthquake sorted by source-to-station azimuth and aligned at the first-arrived phase (*hatched line*). The three common pulses (T1, T2, and T3) employed in the directivity method are identified by *vertical lines* in each seismogram and are listed in Table 4

3. Zemmouri–Boumerdes, Algeria ($M_w = 6.8$; May 21, 2003)

Thirty waveforms separated by an average angular interval of 12° and a major gap of 45° east of the epicenter, between stations LSA and KMBO, were considered (Table 5). Three common pulses were identified, T1, T2, and T3 (Fig. 17), which explain the rupture during the first 12 s; the pulses were considered to have a reading error of 1.5 s.

4. Sumatra, Indonesia ($M_w = 9.3$; December 26, 2004)

For the directivity study of the Sumatra earthquake, 47 waveforms from stations spanning an azimuthal coverage with an average angular interval of 6.7° and a major gap of 35.36° south-southwest of the epicenter, between the AIS and SUR stations (Table 6), were selected. The five pulses selected on the seismograms presented in Fig. 18 follow the rupture propagation during the first 250 s. We estimated the reading errors in the seismograms to be 2.5 s.

Fig. 17 Vertical P waveforms from the 2003 Zemmouri–Boumerdes (Algeria) earthquake sorted by source-to-station azimuth and aligned at the first-arrived phase (*hatched line*). The three common pulses (T1, T2, and T3) employed in the directivity method are identified by *vertical lines* in each seismogram and are listed in Table 5

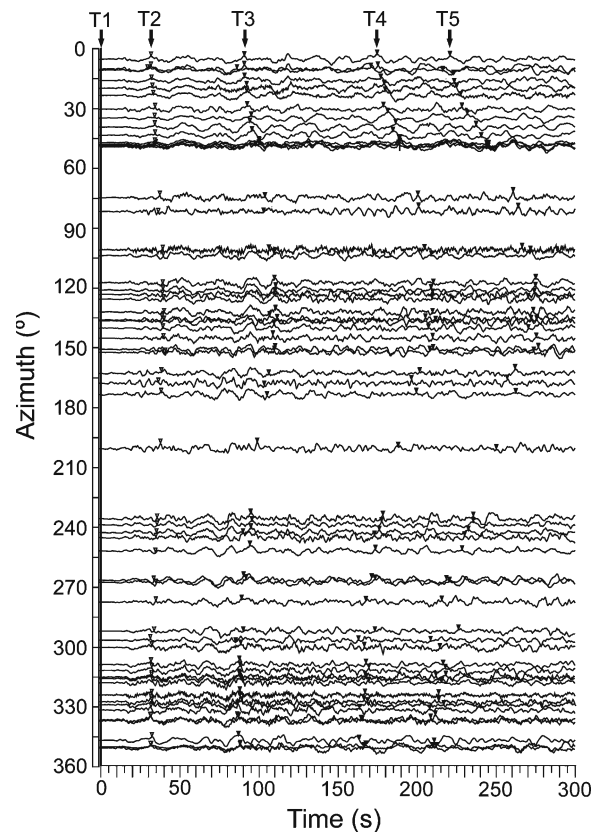
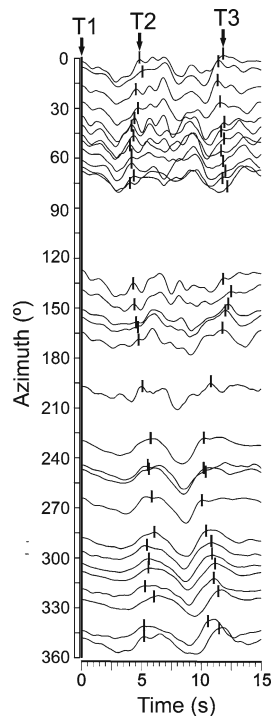


Fig. 18 Vertical P waveforms from the 2004 Sumatra (Indonesia) earthquake sorted by source-to-station azimuth and aligned at the first-arrived phase (*hatched line*). For each seismogram, five common pulses (T1, T2, T3, T4, and T5) employed in the DIRDOP method are identified by the *inverted triangles*. The intervals between the identified pulses, which vary smoothly as a function of azimuth, are listed in Table 6

4.2 Results

The results of applying the method to these earthquakes are represented in Figs. 19, 20, 21, 22, 23, and 24 and are listed in Table 7. For the intervals considered (D_i ; $i = 1, 2, 3, \dots$), the upper part of Figs. 19–23 shows the azimuthal projection map with the position of each station used and, by isolines, the pulse-time measured in the seismograms, interpolated into each location. The arrows represent the estimated directions for the sections of the rupture. The lower part of Figs. 19–23 shows, as a function of the azimuth from the epicenter, (a) time delays read in seismograms, (b) normalized time delays for an

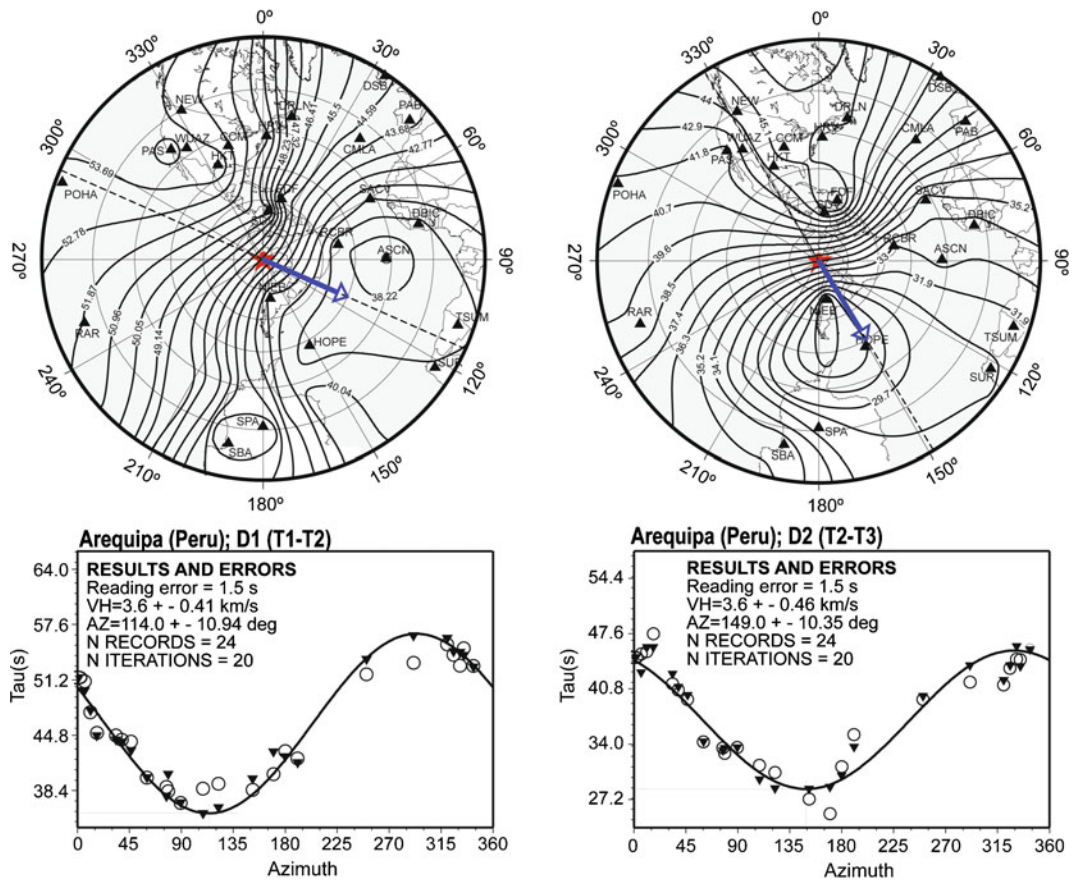


Fig. 19 Directivity results for the Arequipa (Peru) earthquake from the two intervals considered in Fig. 15 and Table 3, D1 (left) and D2 (right). The upper plots show, on an azimuthal projection map centered at the Arequipa earthquake focus, the interpolated spatial distribution (isolin) of the common phase delays. Shaded triangles mark the stations used, and the arrows mark the calculated rupture direction. The lower plots show the phase delay versus azimuth for the intervals D1 and D2. Open circles

and solid inverted triangles represent the time between common pulses measured in seismograms and the corresponding normalized times (for fixed epicentral distance 66.8°), respectively. The solid line represents the predicted time delay distribution, which was obtained by inverting the directivity model. The highest correlation coefficient occurs at an azimuth of 114° (minimum of the curve) for interval D1 and 149° for interval D2. The corresponding results are listed in Table 7

epicentral distance, and (c) the fit to the normalized times obtained by DIRDOP. The numerical results that correspond to the fits of Figs. 19–23 are shown in Table 7. Finally, we are able to easily compare our results, for each case study, with those obtained previously by other authors (Table 7):

1. Arequipa, Peru ($M_w = 8.4$; June 23, 2001)

For the Arequipa earthquake, the initial rupture (first 50 s) occurs toward the ESE ($\gamma = 114.0 \pm 11.0^\circ$, segment D1) and a second segment of the

rupture (next ~30 s) turns toward the S ($\gamma = 149.0 \pm 10.4^\circ$, segment D2). The rupture velocity in both segments is 3.6 km/s (Fig. 19). From these results, it is possible to explain the first 82 s of the rupture, which corresponds to about 295 km of the fault. These results, similar to those obtained with different methods in other studies, suggest that the rupture occurred on plane A of the focal mechanism represented in Fig. 14. Bilek and Ruff (2002) analyzed the relative source time function durations obtained from surface wave data and found a rupture azimuth of $\gamma = 116^\circ$.

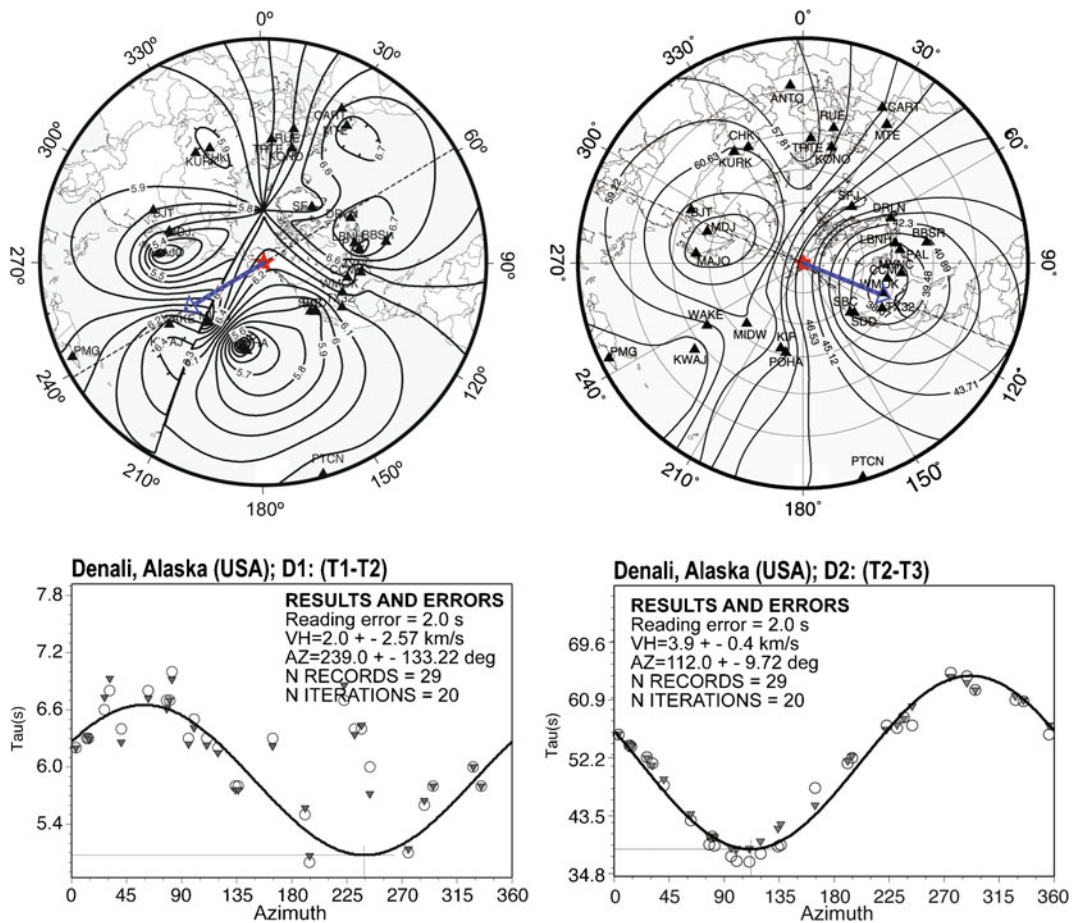


Fig. 20 Directivity results for the Denali (AK, USA) earthquake from the two intervals shown in Fig. 16 and listed in Table 4. The *upper plots* show, on an azimuthal projection map centered at the Denali (AK, USA) earthquake focus, the interpolated spatial distribution (isolines) of the common phase delays. *Shaded triangles* mark the stations used, and *arrow* marks the calculated rupture direction. The *lower plots* show the phase delay versus azimuth for the D1 intervals. *Open circles* and *solid inverted*

triangles represent the time between common pulses measured in seismograms and the related normalized times (for the fixed epicentral distance), respectively. The *solid line* represents the predicted time delay distribution, which was obtained by inverting the directivity model. The highest correlation coefficient occurs at an azimuth of 239° (minimum of the curve) for interval D1 and 112° for interval D2. The corresponding results are listed in Table 7

Robinson et al. (2006), applying the linear programming method of Das and Kostrov (1990), showed a unilateral rupture that propagated from northwest to southeast with an average rupture velocity of 3.5 km/s, corresponding with the result obtained by DIRDOP (3.6 km/s). The results of Le Pichon et al. (2002) obtained by analysis of the ground-coupled air waves show that the rupture propagated southeast at a rupture velocity of 3.3 ± 0.3 km/s with a source duration of 90 ± 10 s. Pritchard et al. (2007) determined the spatiotem-

poral slip distribution using a joint inversion of teleseismic, geodetic, and strong-motion data, and two average rupture directions can be seen, as in the DIRDOP results, although with slightly different azimuths. From the Pritchard slip distribution, the azimuth of the two segments of rupture are $\gamma_1 = 127^\circ$ and $\gamma_2 = 176^\circ$; DIRDOP method gives $\gamma_1 = 114.0 \pm 10.94$ and $\gamma_2 = 149.0 \pm 10.35$. In the work of Pritchard et al. (2007), they obtained an average rupture velocity value of 2.7 km/s.

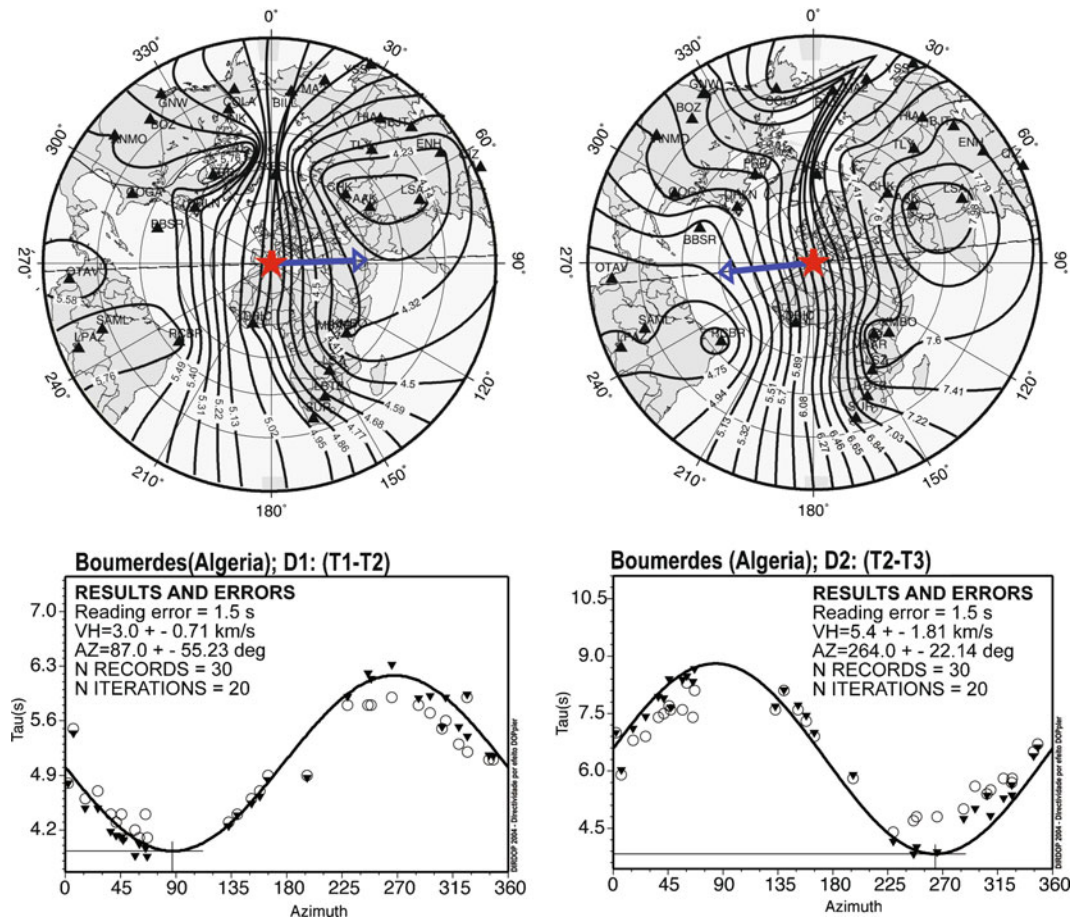


Fig. 21 Directivity results for the Zemmouri–Boumerdes (Algeria) earthquake for the two intervals considered in Fig. 17 and Table 5, D1 (left) and D2 (right). The upper plots show, on an azimuthal projection map centered at the Zemmouri–Boumerdes (Algeria) earthquake focus, the interpolated spatial distribution (isolines) of the common phase delays. Shaded triangles mark the stations used, and the arrow marks the calculated rupture direction. The lower plots show the phase delay versus azimuth for the D1

and D2 intervals. Open circles and solid inverted triangles represent the time between common pulses measured in seismograms and the related normalized times (for fixed epicentral distance), respectively. The solid line represents the predicted time delay distribution, which was obtained by inverting the directivity model. The highest correlation coefficient occurs at an azimuth of 87° (minimum of the curve) for interval D1 and 264° for interval D2. The corresponding results are listed in Table 7

The direction and length of the D1 and D2 segments, estimated from the times used and respective rupture velocity found, are projected on the map of Fig. 24a, which also shows the slip distribution detected by Pritchard et al. (2007). Table 7 compares all these values.

2. Denali, AK, USA ($M_w = 7.8$; November 3, 2002)

For the Denali (AK, USA) earthquake, the results that correspond to the sections of break that

occurred in the intervals ~0–5 and ~5–55 s are represented in Fig. 20 and Table 7. These intervals correspond mainly to the first and second sections of the rupture along the Susitna Glacier fault and Denali fault, as observed in other studies (e.g., Eberhart-Phillips et al. 2003; Ozacar and Beck 2004). The results showed that the first ~5 s (D1) are derived from a dataset that does not produce a good fit to the theoretical model (Fig. 20). Consequently, high values of error were found in both the rupture velocity (2.0 ± 2.57 km/s) and the

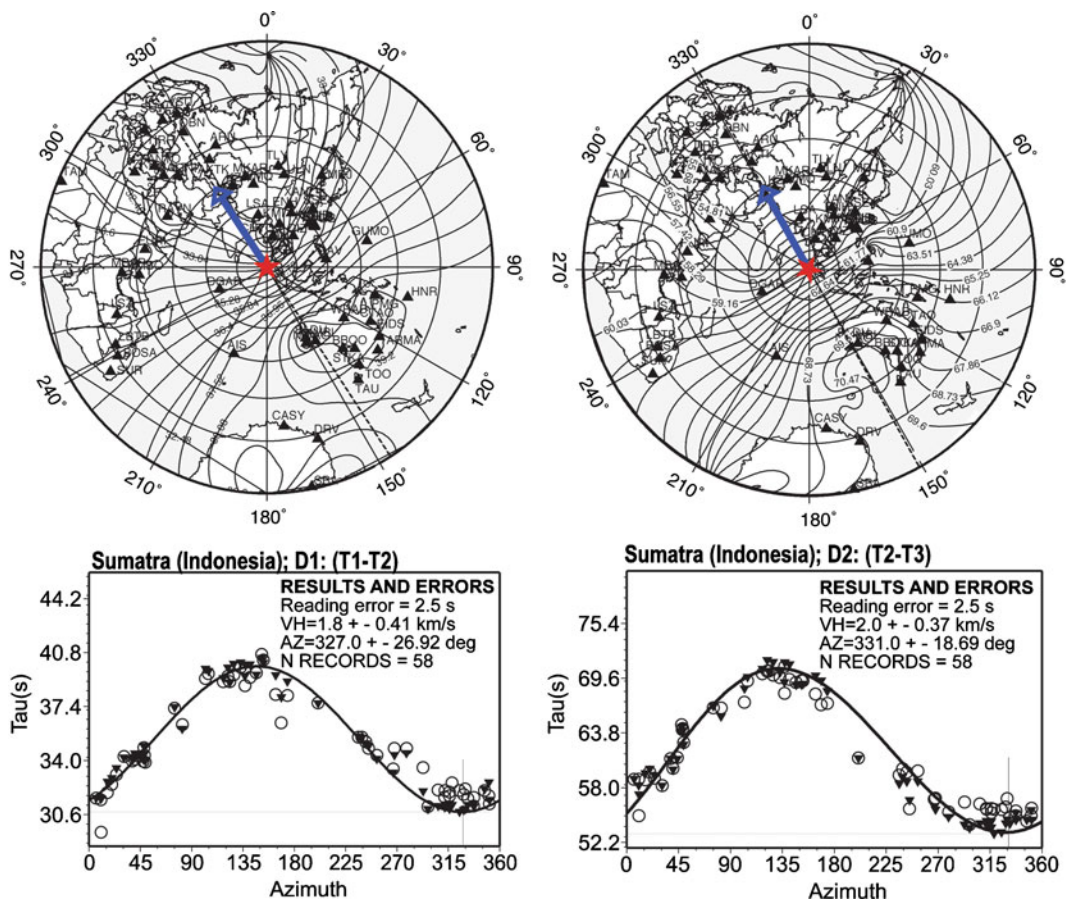


Fig. 22 Directivity results for the Sumatra (Indonesia) earthquake from the two first of four intervals considered in Fig. 18 and Table 6, D1 (left) and D2 (right). The upper plots show, on an azimuthal projection map centered at the Sumatra (Indonesia) earthquake focus, the interpolated spatial distribution (isolines) of common phase delays. Shaded triangles mark the stations used, and the arrow marks the calculated rupture direction. The lower plots show the phase delay versus azimuth for the D1 and D2

intervals. Open circles and solid inverted triangles represent the time between common pulses measured in seismograms and the related normalized times (for the fixed epicentral distance), respectively. The solid line represents the predicted time delay distribution, which was obtained by inverting the directivity model. The highest correlation coefficient occurs at an azimuth of 327° (minimum of the curve) for interval D1 and 331° for interval D2. The corresponding results are listed in Table 7

direction ($\gamma = 239.0 \pm 2.57$ km/s). As discussed above (results of the synthetic C2), this behavior suggests that the section of the rupture that corresponds to the first 5 s is bilateral. This conclusion is consistent with the models presented by Eberhart-Phillips et al. (2003) or Dunham and Archuleta (2004), who describe this rupture with emerging bilateral to unilateral change after the first few seconds. The next ~ 50 s shows a unilateral rupture, with a length estimated to be 273 km toward the ESE with an azimuth of $\gamma = 112 \pm 7.27^\circ$. This suggests that the rupture corresponds

to plane A of the focal mechanism represented in Fig. 14 and adjusts with those determined from the teleseismic body waveform inversion (Kikuchi and Yamanaka 2002; Ozacar and Beck 2004) or strong-motion waveforms (Eberhart-Phillips et al. 2003; Frankel 2004). An average rupture velocity of 3.9 km/s was found in this study that can be compared with the 3.5 km/s determined from the inversion of strong-motion waveforms by Frankel (2004) and Eberhart-Phillips et al. (2003). Velasco et al. (2004), who investigated the directivity of this earthquake by analyzing the

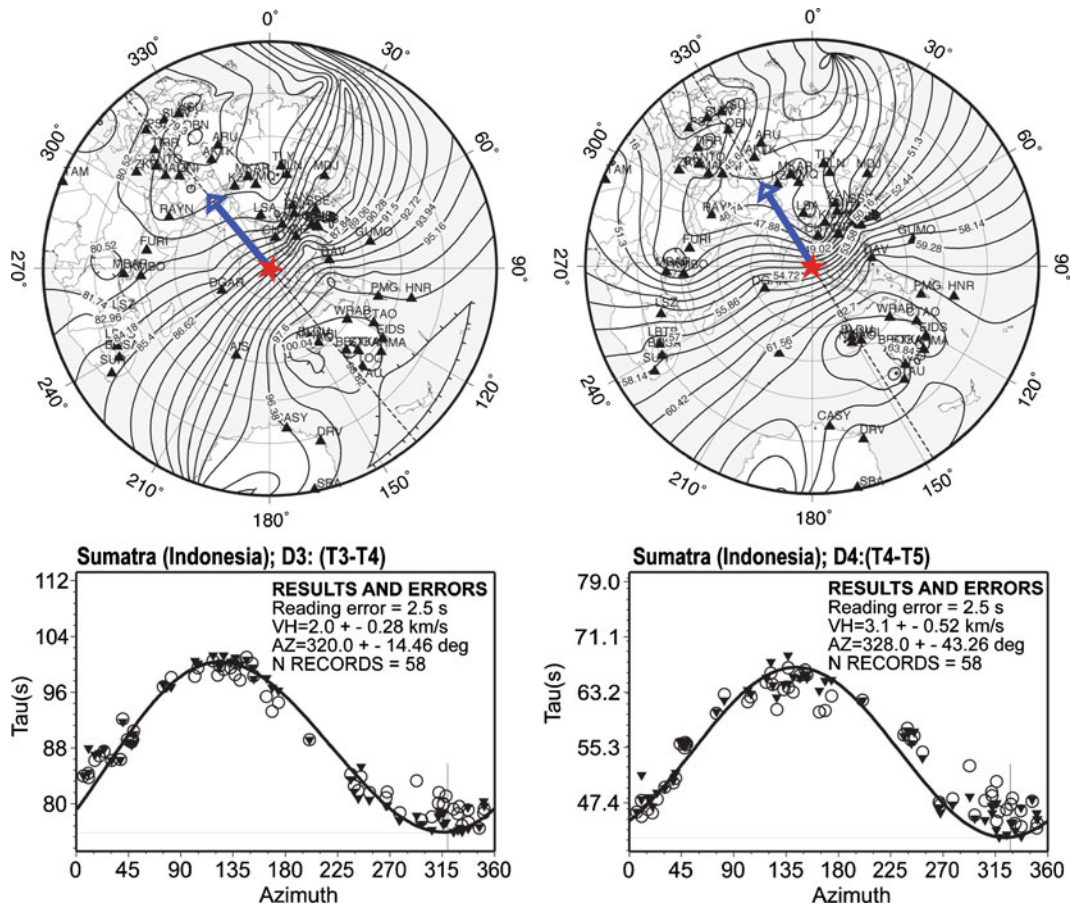


Fig. 23 Directivity results for the Sumatra (Indonesia) earthquake from the two last of four intervals considered in Fig. 18 and Table 6, D3 (left) and D4 (right). The upper plots show, on an azimuthal projection map centered at the Sumatra (Indonesia) earthquake focus, the interpolated spatial distribution (isolines) of common phase delays. Shaded triangles mark the stations used, and the arrow marks the calculated rupture direction. The lower plots show the phase delay versus azimuth for the D3

and D4 intervals. Open circles and solid inverted triangles represent the time between common pulses measured in seismograms and the related normalized times (for fixed epicentral distance), respectively. The solid line represents the predicted time delay distribution, which was obtained by inverting the directivity model. The highest correlation coefficient occurs at an azimuth of 320° (minimum of the curve) for interval D3 and 328° for interval D4. The corresponding results are listed in Table 7

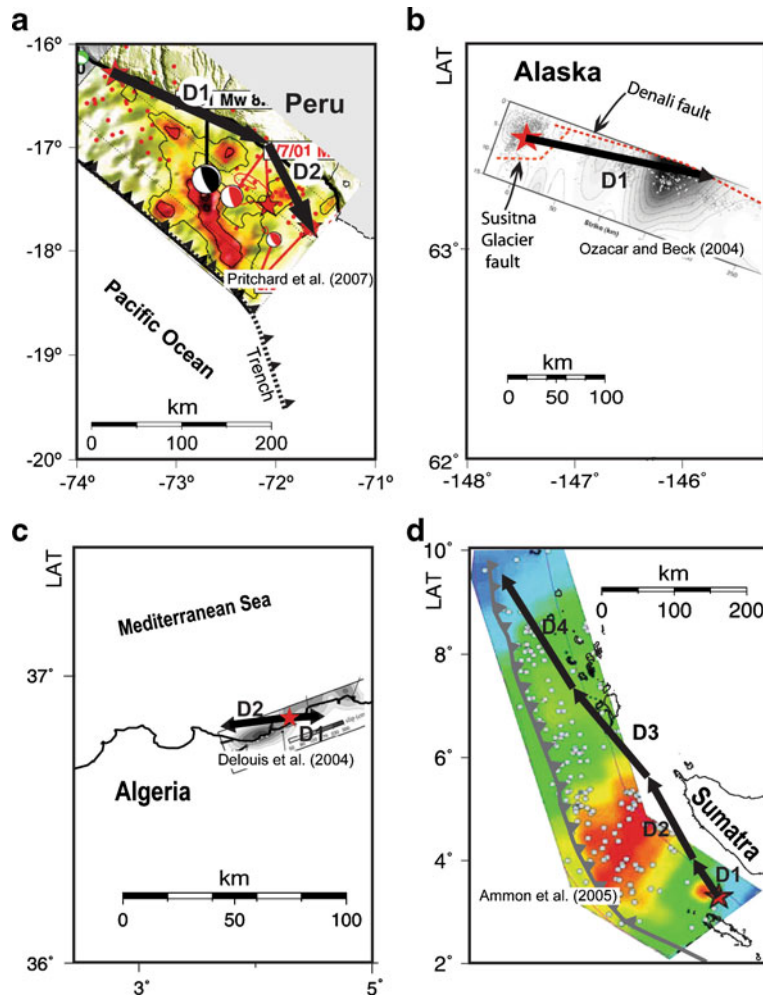
surface wave-amplitude and pulse-width variations of the relative source time functions calculated by the empirical Green functions method, found $\gamma = 122 \pm 25^\circ$ and a rupture velocity of 3.2 km/s. Liao and Huang (2008), using the inversion of the empirical Green’s function, found a unilateral source rupture with a total duration 74 s and a rupture velocity with a maximum of 3.32 km/s and a minimum of 2.64 km/s (the average rupture velocity was about 2.95 km/s). The azimuth of the rupture was approximately 130°.

A comparison with the other studies is laid out in Table 7. The direction of the rupture and the respective length, estimated from the time interval and rupture velocity, are shown in Fig. 24b, which overlap the slip distribution proposed by Ozacar and Beck (2004).

3. Zemmouri–Boumerdes, Algeria ($M_w = 6.8$; May 21, 2003)

In the case of the Zemmouri–Boumerdes (Algeria) earthquake, the results show a bilateral rupture in the E–W direction (Fig. 21) and suggest

Fig. 24 Summary of the front expansion for the four studied earthquakes inferred from the directivity results listed in Table 7: **a** the Arequipa (Peru) earthquake, **b** the Denali (AK, USA) earthquake, **c** the Zemmouri–Boumerdes (Algeria) earthquake, and **d** the Sumatra (Indonesia) earthquake. The *red star* marks the epicenter, and the *black arrows* represent the average direction and the extent of the rupture front during the related period. For each situation, the results of DIRDOP are compared with significant results published by the authors referenced



that the rupture corresponds to plane A of the focal mechanism represented in Fig. 14. In the first 5 s (segment D1), the rupture propagates from the epicenter toward the east ($\gamma = 87.0 \pm 55.23^\circ$) at an average velocity of 3.0 ± 0.71 km/s. In the last 10 s, the rupture propagates at an average velocity of 5.4 ± 1.81 km/s but in the opposite direction ($\gamma = 264 \pm 22^\circ$; segment D2). The bilaterality of the rupture was also reported by Yagi (2003), Delouis et al. (2004), Semmane et al. (2005), and Belabbès et al. (2009). Yagi (2003) found an asymmetric bilateral rupture that mainly propagated 30 km to the southwest and 20 km to the northeast. Delouis et al. (2004), by joint inversion of teleseismic waveforms and global positioning system (GPS) data, estimate two slip zones, on both sides (NE and SW) of the

hypocenter, and low rupture velocity (2.4 km/s in NE section and 1.9 km/s in SW section). Semmane et al. (2005), using an inversion analysis of strong-motion and GPS data, fixed the fault orientation (USGS CMT), and the slip distribution result also reveals the two patches of a bilateral rupture. Belabbès et al. (2009) studied the surface deformation associated with the May 21, 2003 Zemmouri (Algeria) earthquake by inversion of InSAR, coastal uplift, and GPS data and found two rupture sections on both sides of the epicenter. The direction of each segment and the respective length, estimated from the time interval and rupture velocity, are shown in Table 7 and Fig. 24c which also shows, in overlap, the slip distribution calculated by Delouis et al. (2004).

Table 7 Summary of results

Event	Section considered	Rupture azimuth (deg)	Rupture velocity (km/s)	Authors
Arequipa (Peru) 2001	D1 (0–50 s)	114.0 ± 10.94	3.6 ± 0.41	This work
	D2 (50–82 s)	149.0 ± 10.35	3.6 ± 0.46	
	All rupture	116	–	Bilek and Ruff (2002)
	All rupture 0–50 s	–	3.5	Robinson et al. (2006)
	50–80 s	127 ^a	2.7	Pritchard et al. (2007)
	All rupture (~90 s)	–	3.3 ± 0.3	Le Pichon et al. (2002)
Denali (AK, USA) 2002	D1 (0–5 s)	239.0 ± 133.2	2.0 ± 2.57	This work
	D2 (5–55 s)	112.0 ± 7.27	3.9 ± 0.4	
	All rupture	122.0 ± 25	3.2	Velasco et al. (2004)
	–	–	3.5	Frankel (2004)
	~0–20 s	90	3.2	Ozacar and Beck (2004)
	~20–120 s	110		
	Along Susitna Glacier fault (~40 km)		3.5	Eberhart-Phillips et al. (2003)
	Along Denali fault (~200 km)			
	Along Totschunda fault (~60 km)			
	First 30 s	47	3	Kikuchi and Yamanaka (2002)
Last 70 s	114			
All rupture (74 s)	130	2.95	Liao and Huang (2008)	
Zemmouri–Boumerdes (Algeria) 2003	D1 (0–5 s)	87.0 ± 55.23	3.0 ± 0.71	This work
	D2 (5–10 s)	264.0 ± 22.0	5.40 ± 1.81	
	30 km	SW	–	Yagi (2003)
	20 km	NE	–	
	30 km	70	2.0–2.4	Delouis et al. (2004)
	24 km	250	1.6–1.9	
	38 km	58	2.8	Semmane et al. (2005)
	26 km	238		
	~30 km	65	–	Belabbès et al. (2009)
	~30 km	245	–	
Sumatra (Indonesia) 2004	D1 (0–35 s)	327.0 ± 16.92	1.8 ± 0.31	This work
	D2 (35–100 s)	331.0 ± 8.69	2.0 ± 0.17	
	D3 (100–180 s)	320.0 ± 5.98	2.0 ± 0.11	
	D4 (180–240 s)	328.0 ± 12.98	3.1 ± 0.18	
	0–60 s	Parallel to trench direction	1.7–2.2	Krüger and Ohrnbergers (2005b)
	60 s–final		2.5–3.5	
	All rupture 0–60 s	310–330°	2.5	Ammon et al. (2005)
	60 s–final		~1.3	
	All rupture (550 s)	–	~3.0	
	All rupture	Parallel to trench direction	2.3	Lambotte et al. (2007)
	All rupture	Parallel to trench direction	2.0–3.0	Lay et al. (2005)
	All rupture (8 min)	Aftershock zone	2.8	Ishii et al. (2005)
	All rupture	Parallel to trench direction	1.8–2.8	Rhie et al. (2007)
	All rupture (1,200 km)	Parallel to trench direction	2.2 ± 0.1	Vallée (2007)
	First 100 km		1.8	
100–500 km		2.4–2.5		
500 km–final		2		

Summary of the direction and velocity of the rupture and errors obtained in this work corresponding to each considered time interval of each earthquake studied and the same parameters calculated by other authors

^aEstimated from slip distribution

4. Sumatra, Indonesia ($M_w = 9.3$; December 26, 2004)

In the case of the Sumatra mega-earthquake, the results corresponding to the fits shown in Figs. 22 and 23 are represented in Table 7. These results suggest that the rupture corresponds to plane A of the focal mechanism represented in Fig. 14 and shows that (1) the rupture started slowly ($v_r = 1.8 \pm 0.11$ km/s) in the first 35 s (segment D1), occurring mainly toward the NW, $\gamma = 327 \pm 26.9^\circ$ direction; the low value obtained for the rupture velocity in this interval suggests a bilateral circular rupture that corresponds to the nucleation; (2) during 35 to 100 s (segment D2), the rupture propagates in the $\gamma = 331 \pm 18.7^\circ$ direction with a moderate rupture velocity ($v_r = 2.0 \pm 0.37$ km/s); (3) in the third time interval, between 100–180 s (segment D3), the rupture expands in the $\gamma = 320 \pm 14.4^\circ$ direction with a $v_r = 2.0 \pm 0.28$ km/s; and (4) finally, in the last interval analyzed by this method, 180–240 s (segment D4), the rupture continues expanding in the north–northwest direction ($\gamma = 328 \pm 43.26^\circ$) but exhibits a higher velocity ($v_r = 3.1 \pm 0.52$ km/s). The direction of each segment and the correspondent rupture velocity are shown in Table 7. By way of the directivity results, it is possible to explain only the first 240 s of the rupture, which correspond to about 540 km of length. It was impossible to identify common pulses after this time due to the interference of later-arriving seismic waves reflected from the surface and discontinuities in the Earth, with P waves radiating from later portions of the rupture. This limitation of the study of large earthquakes is common in methods that involve the analysis of extended portions of seismic body waveforms. Details of the rupture velocity show that the propagation is much slower in the first stage of the rupture process (first 60 s) and accelerates to 3.1 km/s from that point onward. The very slow velocity during the first 60 s (1.8 km/s) may be associated with the bilateral or circular character of the first phase of the rupture. The direction of each segment and the respective length estimated from the time interval and rupture velocity are shown in Fig. 24c, which also shows the slip distribution detected by Ammon et al. (2005).

Similar results, listed in Table 7, were obtained by other authors. Krüger and Ohrnberger (2005b) show that the rupture started rather slowly for the first 60 s (average rupture velocity between 1.7 and 2.2 km/s) and then accelerated to a more constant level between 2.5 and 3.5 km/s. Ammon et al. (2005) proposed an average rupture velocity of 2.5 km/s along a rupture direction of 310° to 330° . Lambotte et al. (2007) deduced an average rupture velocity of about 2.3 ± 0.3 km/s from the spatiotemporal results (length of approximately 1,250 km and duration of approximately 550 s). Lay et al. (2005) found the variable velocity to be between 2.0 and 3.0 km/s. Ishii et al. (2005) mapped the rupture spread northward at a velocity of roughly 2.8 km/s for approximately 8 min. Rhie et al. (2007) determined rupture velocities between 1.8 and 2.8 km/s. Vallée (2007) found an average rupture velocity of 2.2 km/s (± 0.1) that was unequally distributed throughout three sections: (1) the first 100 km with ~ 1.8 km/s, (2) accelerating to values of 2.4–2.5 km/s for the next 500 km, and (3) decelerating to 2 km/s in the second half of the rupture process.

5 Discussion and conclusions

The purpose of the seismic source investigation is to obtain an accurate description of the rupture from seismic data. Geodesic records can sometimes facilitate this process. The success of this depends fundamentally on three factors: source models, informative content of the data, and the methods used. Currently, seismic wave inversion techniques are considered better methods for obtaining rupture characteristics from seismic data. This is a delicate problem because of the number of parameters needed for estimation and the nonlinear setting in which the problem develops. The accuracy of the inversion solutions depends largely on the correct choice of the free and fixed parameters of the method; if the fixed parameters are few and their values are adequately chosen (guided by other methods and data), the process of obtaining the solution can be controlled substantially. The evaluation of directions and velocities for seismic ruptures is an important problem

in the field of the finite seismic source. We note that even when rupture velocity values are calculated, their corresponding directions generally remain undetermined. They are fixed by considerations of the geometry of faults or by considering one of the planes of the focal mechanism. The approach described provides a tool that, using Doppler interpretation, allows for the estimation of the rupture vector velocity. The ability to determine these parameters from a simple analysis of the seismic data is a very useful outcome of this method because these parameters are difficult to calculate using other methods. Sometimes the velocities of rupture are simply fixed in the accepted band (2.4–3.6 km/s). However, theoretical studies (e.g., Day 1982) reveal the possibility of a wider band. In fact, in the Izmith (Turkey) earthquake of 1999, rupture velocities of 5.8 km/s (Sekiguchi and Iwata 2002) and 4.8 km/s (Bouchon et al. 2002) were detected.

The methodology presented here can use data obtained directly by identifying common pulses in the azimuthal distributions of seismograms, as well as data obtained from other sources of rupture information. Two of these other sources are the RSTF and the body waves amplitude spectra diagrams. In RSTF, the intervals between common marks are used, whereas in the spectra diagrams, we use corner frequencies. The quality of the results depends on the accuracy of the phase identification and azimuthal coverage. The estimates of error obtained by this method depend strongly on azimuthal gaps in the data, especially if these gaps coincide with the directions of the extrema of the model (Eq. 6).

This method can be applied to any unilateral earthquake, depending only on whether it is possible to identify common pulses. It can be used for small earthquakes, provided that the following two conditions are met: (a) it is possible to identify common pulses in all seismograms and (b) the measured time-delays are perceptible, i.e., they are at least one order of magnitude greater than the uncertainties. For small events, however, it is difficult to apply the method, mainly for two reasons. First, the seismograms need to be acquired at short distances, where it is not common to have a dense azimuthal coverage. Second, considering the short source time duration of small

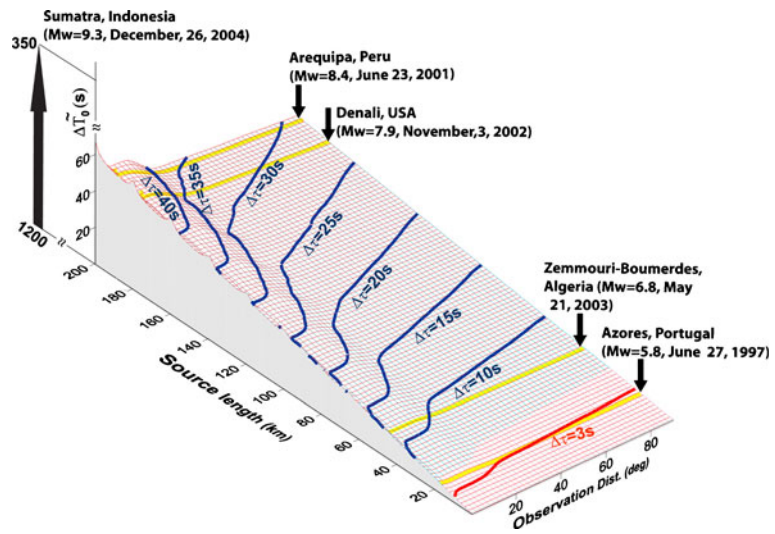
earthquakes, directivity effects are less clear in the seismograms;

If we consider that the two commonly selected pulses in an azimuthal distribution of waveforms correspond to the two ends of the rupture, the time delay between these two pulses is equal to the apparent source time rupture \tilde{T}_0 . From Eq. 12, we conclude that the maximum difference between relative time durations measured in the records is found for a pair of observation points, where one point is aligned with the rupture direction ($\theta = 0$) and the other lies in the opposite direction ($\theta = 180^\circ$).

$$\Delta \tilde{T}_{\max} = \tilde{T}_0(180, p) - \tilde{T}_0(0, p) = 2L \frac{p}{R_0}$$

Figure 25 shows the distribution of $\Delta \tilde{T}_{\max}$ as a function of the observation distance and rupture dimension. It also indicates the predicted differences in five moderate and large earthquakes. Let us note, in Fig. 25, that the four earthquakes studied herein are situated above the discriminatory limit. The Boumerdes (Algeria) earthquake is situated close to this limit. In the Arequipa earthquake, for an observation distance of 20° , $\Delta \tilde{T}_{\max} \approx 50$ s is expected, whereas for 80° , $\Delta \tilde{T}_{\max} < 40$ s. If we suppose that the experimental discriminatory limit between directive and antidirective records is about 3 s, the directivity of events like the Azores earthquake of July 9, 1998 ($M_w = 5.8$) can only be studied using data from distances of less than 20° . However, there are rarely enough stations at these short distances to provide good azimuthal coverage. For very large earthquakes (like Sumatra), these restrictions do not apply; however, other factors complicate the extensive use of the methodology. The records of very extensive seismic ruptures from a certain moment will be composed of many phases that arise from various points of rupture. The interference of these phases will eventually erase the common marks being sought, and the methodology cannot be applied. Ten synthetic scenarios of common unilateral and bilateral ruptures were used to test the efficiency of the methodology to estimate the direction and velocity of the rupture under the control of various parameters, such as the focal mechanism, complexity of the rupture, azimuthal coverage, velocity of the rupture, and

Fig. 25 Limits of the application of the method. 3D plot of the theoretical difference between relative time durations measured from directive and antidirective directions versus observation distance and rupture length for unilateral ruptures. As an example, the values of $\Delta \tilde{T}_0$ are shown for five real earthquakes



laterality of the rupture. We conclude that, in unilateral scenarios, the errors associated with the rupture direction and rupture velocity depend on the angular coverage of the stations (comparing scenarios C1 and C3). The error associated with the rupture direction is, in general, of the same order of magnitude as the maximum azimuthal gap. The methodology is insensitive to changes to the focal mechanism (comparison of scenarios S1, S2, and S3). Low rupture velocity produces directivity marks, which are less obvious on seismograms but are still identifiable. However, the parameters estimated present a larger disparity (comparing scenarios C3 and C4). The results from the bilateral section of scenario C2 show an evident mismatch between the dataset and the theoretical model that could explain the high level of error found. We suggest interpreting these kinds of results as a bilaterality indicator. The results of complex scenarios (C1, C3, and C4) show that, systematically, the estimates of the first section of rupture have lower error rates than subsequent sections. We believe this is due to the increased interference along the seismic record.

The results obtained from the dataset of the four earthquakes analyzed agreed, in general, with the values presented by other authors using different methods and data (Table 7). The analysis of the rupture direction that this methodology allows us to estimate is one of the few simple options available to certify, between the two planes of

focal mechanism, which corresponds to the rupture. Some of the observations made from the synthetic data are confirmed by real data. We found a bilateral rupture in section D1 of the November 3, 2002, Denali, AK, USA ($M_w = 7.8$) earthquake from a dataset that does not produce a good fit with the theoretical model through a similar analysis used in the synthetic C2 scenario. For the four earthquakes studied, it was possible to detect changes both in the direction of the rupture and in its speed.

One of the most sensitive parts of this study is the accurate determination of the time of arrival of common pulses. To avoid this problem, we are developing a method based on the “analysis in the frequency along the time domain”.

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Appendix

Table 8 Common time delays measured on the seismograms in Figs. 6, 7, and 8 used for the synthetic tests (Figs. 10, 11, and 12)

Observation points		Time intervals reads in synthetic seismograms of each scenario (s)										
#	ϕ (deg)	S1	S2	S3	S4	S5	S6		C1		C2	
							I	II	Part I	Part II	Part I	Part II
1	0	8.1	6.9	7.0	8.3	7.7	7.7	9.8	48.8	43.3	15.8	21.6
2	15	7.5	6.9	7.1	7.7	7.7	7.1	10.2	46.6	41.8	16.4	23.4
3	30	7.3	7.1	7.1	7.7	7.6	6.6	10.5	44.0	39.9	16.6	25.2
4	45	7.0	7.2	7.3	7.7	7.5	6.3	10.8	42.1	37.1	16.8	26.7
5	60	6.9	7.6	7.8	7.2	7.4	6.0	11.0	39.6	35.3	17.9	27.5
6	75	6.9	8.1	8.0	7.4	7.7	6.0	11.0	37.3	33.2	17.7	29.2
7	90	7.0	8.6	8.4	7.7	8.0	6.3	10.8	35.7	31.9	17.7	30.6
8	105	7.3	9.3	8.8	8.0	7.9	6.7	10.6	34.4	31.2	17.7	31.6
9	120	7.6	9.7	9.6	7.9	8.7	7.1	10.2	33.6	30.6	17.9	31.9
10	135	7.9	10.2	10.3	8.6	8.8	7.7	9.8	33.1	30.9	17.8	31.9
11	150	8.7	10.5	10.6	8.7	9.3	8.5	9.2	33.6	30.6	17.7	31.9
12	165	9.2	10.7	10.8	9.3	9.6	9.2	8.6	34.7	32.1	17.7	30.9
13	180	9.7	10.8	10.9	9.8	9.8	9.8	7.7	36.5	32.3	17.5	30.2
14	195	10.1	10.8	10.8	9.9	10.0	10.2	7.0	38.4	34.8	17.2	29.1
15	210	10.5	10.7	10.8	10.1	10.2	10.4	6.5	40.6	36.3	17.3	27.7
16	225	10.6	10.5	10.6	10.5	10.4	10.5	6.4	42.9	38.4	17.0	25.6
17	240	10.7	10.1	10.2	10.9	10.0	10.6	6.3	45.3	40.7	16.4	24.7
18	255	10.7	9.9	9.6	10.3	10.0	10.6	6.3	47.5	42.2	16.6	22.7
19	270	10.6	9.4	8.9	10.3	9.9	10.5	6.4	49.5	43.5	16.7	20.9
20	285	10.5	8.7	8.5	10.2	9.4	10.4	6.5	50.9	44.5	16.4	20.5
21	300	10.0	8.0	8.2	9.9	9.1	10.2	7.0	51.7	45.1	16.4	19.9
22	315	9.7	7.6	7.8	9.6	8.9	9.8	7.7	51.8	45.3	16.3	19.9
23	330	9.3	7.3	7.4	9.3	8.6	9.2	8.6	51.1	45.1	15.8	20.3
24	345	8.7	7.0	7.2	8.9	7.9	8.4	9.2	50.2	44.3	15.5	21.3

Table 9 Common time delays measured on the seismograms of Fig. 9 and used for the synthetic seismograms shown in Fig. 13

Observation points			Time intervals reads in synthetic seismograms of each scenario (s)			
Name	Azimuth (deg)	Δ (deg)	C3		C4	
			Part I	Part II	Part I	Part II
HRV	1.5	58.7	58.5	27.1	47.4	56.7
SDV	6.2	25.2	59.1	27.5	48.1	57.8
DRLN	11.2	66.9	56.7	27.1	46.8	56.9
FDF	16.8	32.2	57.2	26.6	47.4	57.5
DSB	33.4	89.9	53.6	26.2	46.0	55.3
CMLA	38.5	70.1	53.1	25.6	45.8	55.1
PAB	46.3	84.9	52.3	25.0	45.4	55.2
SACV	60.2	58.1	49.9	23.8	44.8	54.5
DBIC	77.0	71.5	48.9	22.6	44.6	53.6
RCBR	78.6	38.1	46.6	22.0	43.9	52.8
ASCN	89.4	58.1	46.4	22.1	44.3	52.8
TSUM	108.7	85.6	47.8	21.9	43.9	53.3
SUR	122.2	84.8	47.4	21.9	43.9	52.4

Table 9 (continued)

Observation points			Time intervals reads in synthetic seismograms of each scenario (s)			
Name	Azimuth (deg)	Δ (deg)	C3		C4	
			Part I	Part II	Part I	Part II
HOPE	151.7	47.6	44.7	21.2	43.1	49.9
NIEB	169.8	20.3	45.6	21.3	42.5	49.1
SPA	180.0	73.9	50.5	23.6	43.8	51.3
SBA	190.7	80.2	52.0	24.1	44.4	51.5
RAR	250.4	81.0	59.0	25.4	46.3	57.0
POHA	291.1	88.4	60.9	27.3	46.9	57.9
PAS	320.3	66.0	62.1	28.2	47.4	57.8
WUAZ	325.7	63.0	62.1	28.6	47.4	57.5
NEW	331.5	75.3	60.9	28.3	47.4	57.4
HKT	334.7	51.0	62.1	29.3	47.3	59.5
CCM	343.1	56.8	60.9	27.6	47.4	58.2

References

- Ammon CJ, Chen J, Hong-Kie T, Robinson D, Ni S, Hjorleifsdottir V, Kanamori H, Lay T, Das S, Helmberger D, Ichinose G, Polet J, Wald D (2005) Rupture process of the 2004 Sumatra–Andaman earthquake. *Science* 308:1133–1139. doi:[10.1126/science.1112260](https://doi.org/10.1126/science.1112260)
- Aki K, Richards PG (1980) *Quantitative seismology: theory and methods*, vol 2. Freeman and Co., San Francisco
- Ayadi A, et al (2003) Strong Algerian earthquake strikes near capital city. *Eos Trans AGU* 84(50):561–568. doi:[10.1029/2003EO500002](https://doi.org/10.1029/2003EO500002)
- Ayadi A, Dorbath C, Ousadou F, Maouche S, Chikh M, Bounif MA, Meghraoui M (2008) Zemmouri earthquake rupture zone (Mw 6.8, Algeria): aftershocks sequence relocation and 3-D velocity model. *J Geophys Res* 113:B09301. doi:[10.1029/2007JB005257](https://doi.org/10.1029/2007JB005257)
- Baumont D, Courboux F, Scotti O, Melis NS, Stavrakakis G (2002) Slip distribution of the Mw 5.9, 1999 Athens earthquake inverted from regional seismological data. *Geophys Res Lett* 29(1720):15.1–15.4. doi:[10.1029/2001GL014261](https://doi.org/10.1029/2001GL014261)
- Beck S, Silver P, Wallace T, James D (1995) Directivity analysis of the deep Bolivian earthquake of June 9, 1994. *Geophys Res Lett* 22:2257–2260
- Belabbès S, Wicks CZ, Akir C, Meghraoui M (2009) Rupture parameters of the 2003 Zemmouri (Mw 6.8), Algeria, earthquake from joint inversion of interferometric synthetic aperture radar, coastal uplift, and GPS. *J Geophys Res* 114:B03406. doi:[10.1029/2008JB005912](https://doi.org/10.1029/2008JB005912)
- Benioff H (1955) Mechanism and strain characteristics of the white wolf fault as indicated by the aftershock sequence. *Calif Div Mines Bull* 171:199–202
- Ben-Menahem A (1961) Radiation of seismic surface-waves from finite moving sources. *Bull Seismol Soc Am* 51:401–435
- Ben-Menahem A, Singh SJ (1981) *Seismic waves and sources*. Springer, New York
- Beresnev IA (2003) Uncertainties in finite-fault slip inversions: to what extent to believe? (A critical review). *Bull Seismol Soc Am* 93:2445–2458
- Bezzeghoud M, Buforn E (1999) Source parameters of 1992 Melilla (Spain, Mw = 4.8), 1994 Alhoceima (Morocco, Mw = 5.8) and 1994 Mascara (Algeria, Mw = 5.7) earthquakes and seismotectonic implications. *Bull Seismol Soc Am* 89(2):359–372
- Bilham R, Engdahl ER, Feldl N, Satyabala SP (2005) Partial and complete rupture of the Indo-Andaman plate boundary 1847–2004. *Seismol Res Lett* 76(3):299–311. doi:[10.1785/gssrl.76.3.299](https://doi.org/10.1785/gssrl.76.3.299)
- Bilek S, Ruff L (2002) Analysis of the 23 June 2001 Mw = 9.4 Peru underthrusting earthquake and its aftershocks. *Geophys Res Lett* 29(20):21.1–21.4. doi:[10.1029/2002GL015543](https://doi.org/10.1029/2002GL015543)
- Boore D, Joyner W (1978) The influence of rupture incoherence on seismic directivity. *Bull Seismol Soc Am* 68:283–300
- Borges J (2003) *Fonte Sísmica Em Portugal-Algumas Implicações Na Geodinâmica Da Região Açores-Gibraltar*. PhD thesis, Évora University
- Bouchon M, Toksöz N, Karabulut H, Bouin M, Dietrich M, Aktar M, Edie M (2002) Space and time evolution of rupture and faulting during the 1999 Izmit (Turkey) earthquake. *Bull Seismol Soc Am* 92:256–266
- Buforn E, Bezzeghoud M, Udias A, Pro C (2004) Seismic source in the Iberian–African plate boundary. *Pageoph* 161(3):623–646
- Bullen KE, Bolt B (1985) *Introduction to the theory of seismology*. Cambridge University Press, Cambridge
- Caldeira B (2004) *Caracterização espaço-temporal da fonte sísmica—Processos de ruptura e directividade*. PhD thesis, Évora University
- Caldeira B, Bezzeghoud M, Borges J (2004) Contributo da directividade para a caracterização da Fonte do sismo de Boumerdes (Argélia) de 21 de Maio de 2003, Mw =

- 6.7. 4 Assembleia Luso-Espanhola de Geodesia e Geofísica, pp 251–252
- Cipar J (1979) Source processes of the Haicheng, China earthquake from observations of P and S waves. *Bull Seismol Soc Am* 69:1903–1916
- Das S, Kostrov BV (1990) Inversion for seismic slip rate history and distribution with stabilizing constraints application to the 1986 Andean of islands earthquake. *J Geophys Res* 95(B5):6899–6913
- Day S (1982) Three dimensional simulation of spontaneous rupture: the effect of nonuniform pre-stress. *Bull Seismol Soc Am* 72:1881–1901
- Delouis B, Vallée M, Meghraoui M, Calais E, Mahsas S, Briole P, Benhamouda F, Yelles K (2004) Slip distribution of the 2003 Boumerdes–Zemmouri earthquake, Algeria, from teleseismic, GPS, and coastal uplift data. *Geophys Res Lett* 31:L18607. doi:[10.1029/2004GL020687](https://doi.org/10.1029/2004GL020687)
- Douglas A, Hudson J, Pearce R (1988) Directivity and the Doppler effect. *Bull Seismol Soc Am* 78:1367–1372
- Dunham M, Archuleta RJ (2004) Evidence for a super-shear transient during the 2002 Denali fault earthquake. *Bull Seismol Soc Am* 94:S256–S268
- Eberhart-Phillips D, Haeussler P et al (2003) The 2002 Denali fault earthquake, Alaska: a large magnitude, slip-partitioned event. *Science* 300:1113–1118. doi:[10.1126/science.1082703](https://doi.org/10.1126/science.1082703)
- Frankel A (2004) Rupture process of the M 7.9 Denali fault, Alaska, earthquake: subevents, directivity, and scaling of high-frequency ground motions. *Bull Seismol Soc Am* 94:S234–S255
- French AP (1974) *Vibrations and waves*. Norton, New York
- Fukao Y (1972) Source process of a large deep-focus earthquake and its tectonic implications—the western Brazil earthquake of 1963. *Phys Earth Planet Inter* 5:61–76
- Grach SM, Komrakov GP, Yurishchev MA, Thid B, Leyser TB, Carozzi T (1997) Multifrequency Doppler radar observations of electron gyroharmonic effects during electromagnetic pumping of the ionosphere. *Phys Rev Lett* 78(5):883–886. doi:[10.1103/PhysRevLett78.883](https://doi.org/10.1103/PhysRevLett78.883)
- Haskell NA (1964) Total energy and energy spectral density of elastic wave radiation from propagating faults. *Bull Seismol Soc Am* 54:1811–1841
- Hoshiya M (2003) Fluctuation of wave amplitude even when assuming convolution of source, path and site factors—effect of rupture directivity. *Phys Earth Planet Inter* 137:45–65
- Ihmlé PF (1998) On the interpretation of subevents in teleseismic waveforms: the 1994 Bolivia deep earthquake revisited. *J Geophys Res* 103(B8):17,919–17,932
- Ishii M, Shearer P, Houston H, Vidale J (2005) Extend, duration and speed of the 2004 Sumatra–Andaman earthquake imaged by the Hi-Net array. *Nature* 435:933–936. doi:[10.1038/nature03675](https://doi.org/10.1038/nature03675)
- Kasahara K (1981) *Earthquakes mechanics*. Cambridge Univ. Press, Cambridge
- Kennett B, Engdahl E (1991) Traveltimes for global earthquake location and phase identification. *Geophys J Int* 105:429–465
- Kikuchi M, Kanamori H (1991) Inversion of complex body waves—III. *Bull Seismol Soc Am* 81:2335–2350
- Kikuchi M, Yamanaka Y (2002) Source rupture processes of the central Alaska earthquake of Nov. 3, 2002, inferred from teleseismic body waves, EIC Seismological Note. No. 129, Nov. 4
- Kraeva N (2004) Tikhonov's regularization for deconvolution in the empirical green function method and vertical directivity effect. *Tectonophysics* 383:29–44
- Krüger F, Ohrnberger M (2005a) Tracking the rupture of the Mw = 9.3 Sumatra earthquake over 1,150 km at teleseismic distance. *Nature* 435:937–939. doi:[10.1038/nature03696](https://doi.org/10.1038/nature03696)
- Krüger F, Ohrnberger M (2005b) Spatio-temporal source characteristics of the 26 December 2004 Sumatra earthquake as imaged by teleseismic broadband arrays. *Geophys Res Lett* 32:L24312. doi:[10.1029/2005GL023939](https://doi.org/10.1029/2005GL023939)
- Lambotte S, Rivera L, Hinderer J (2007) Constraining the overall kinematics of the 2004 Sumatra and the 2005 Nias earthquakes using the earth's gravest free oscillations. *Bull Seismol Soc Am* 97(1A):S128–S138. doi:[10.1785/0120050621](https://doi.org/10.1785/0120050621)
- Lay T, Kanamori H, Ammon C, Nettles M, Wald SN, Aster RC, Beck S, Bilek S, Brudzinski MR, Butler R, DeShon HR, Ekstrom G, Satake K, Sipkin S (2005) The great Sumatra–Andaman earthquake of 26 December 2004. *Science* 308(5725):1127–1133. doi:[10.1126/science.1112250](https://doi.org/10.1126/science.1112250)
- Le Pichon A, Guilbert J, Vega A, Garce's M, Brachet N (2002) Ground-coupled air waves and diffracted infrasound from the Arequipa earthquake of June 23, 2001. *Geophys Res Lett* 29(18):33.1–33.4. doi:[10.1029/2002GL015052](https://doi.org/10.1029/2002GL015052)
- Liao BY, Huang H (2008) Rupture process of the 2002 Mw 7.9 Denali earthquake, Alaska, using a newly devised hybrid blind deconvolution method. *Bull Seismol Soc Am* 98:162–179. doi:[10.1785/0120050065](https://doi.org/10.1785/0120050065)
- Loupas T, Gill RW (1994) Multifrequency Doppler: improving the quality of spectral estimation by making full use of the information present in scattered RF echoes. *Ultrason Ferroelectr Freq Control* 41(4):522–531. doi:[10.1109/58.294114](https://doi.org/10.1109/58.294114)
- Menke W (1984) *Geophysical data analysis: discrete inverse theory*. Academic, Orlando
- Ni S, Hiro K, Don H (2005) Seismology: energy radiation from the Sumatra earthquake. *Nature* 434:582. doi:[10.1038/434582a](https://doi.org/10.1038/434582a)
- Ozacar AA, Beck SL (2004) The 2002 Denali fault and 2001 Kunlun fault earthquakes: complex rupture processes of two large strike-slip events. *Bull Seismol Soc Am* 94(6B):S278–292. doi:[10.1785/0120040604](https://doi.org/10.1785/0120040604)
- Pritchard M, Norabuena E, Ji C, Boroschek R, Comte D, Simons M, Dixon TH, Rosen PA (2007) Geodetic, teleseismic, and strong motion constraints on slip from recent southern Peru subduction zone earthquakes. *J Geophys Res* 112:B03307. doi:[10.1029/2006JB004294](https://doi.org/10.1029/2006JB004294)
- Pro MC (2002) Estudio del efecto de directividad en la forma de ondas. PhD thesis, Universidad Complutense de Madrid

- Pro C, Buforn E, Udías A (2007) Rupture length and velocity for earthquakes in the Mid-Atlantic Ridge from directivity effect in body and surface waves. *Tectonophysics* 433:65–79
- Rao IS, Anandan VQ, Kumar MS (2009) Multifrequency decoding of a phased array Doppler sodar. *J Atmos Ocean Technol* 26(4):759–768
- Rhie J, Dreger D, Bürgmann R, Romanowicz B (2007) Slip of the 2004 Sumatra–Andaman earthquake from joint inversion of long period global seismic waveforms and GPS static offsets. *Bull Seismol Soc Am* 97(1A):S115–S127
- Russell D, Brucher R (2002) Multifrequency Doppler discriminates between baseous and solid microemboli. *Ann Thorac Surg* 73(1):S369
- Robinson DP, Das S, Watts AB (2006) Earthquake rupture stalled by a subducting fracture zone. *Science* 312:1203–1205
- Semmane F, Campillo M, Cotton F (2005) Fault location and source process of the Boumerdes, Algeria, earthquake inferred from geodetic and strong motion data. *Geophys Res Lett* 32:L01305. doi:[10.1029/2004GL021268](https://doi.org/10.1029/2004GL021268)
- Sekiguchi H, Iwata T (2002) Rupture process of the 1999 Kocaeli, Turkey, earthquake estimated from strong-motion waveforms. *Bull Seismol Soc Am* 92:300–311
- Tavera H, Buforn E, Bernal I, Antayhua Y, Vilacapoma L (2002) The Arequipa (Peru) earthquake of June 23, 2001. *J Seismol* 6(2):279–283
- Tibi R, Estabrook C, Bock G (1999) The 1996 June 17 Flores sea and 1994 March 9 Fiji–Tonga earthquakes: source processes and deep earthquake mechanisms. *Geophys J Int* 138:625–642
- Tregoning P, Brunner FK, Bock YS, Puntodewo SO, McCaffrey R, Genrich JF, Calais E, Rais J, Subarya C (1994) First geodetic measurement of convergence across the Java Trench. *Geophys Res Lett* 21:2135–2139
- Tumarkin A, Archuleta R (1994) Empirical ground motion prediction. *Ann Geofis* XXXVII:1691–1720
- Udias A (1971) Source parameters of earthquakes from spectra of Rayleigh waves. *Geophys J R Astron Soc* 22:253–276
- Vallée M (2007) Rupture properties of the giant Sumatra earthquake imaged by empirical green function analysis. *Bull Seismol Soc Am* 97(1A):S103–S114
- Velasco A, Ammon CJ, Farrell J, Pankow K (2004) Rupture directivity of the 3 November 2002 Denali fault earthquake determined from surface waves. *Bull Seismol Soc Am* 94(6B):S293–S299. doi:[10.1785/0120040624](https://doi.org/10.1785/0120040624)
- Vigny C, Simons W, Abu S, Bamphenyu R, Satirapod C, Choosakul N, Subarya C, Socquet A, Omar K, Abidin HZ, Ambrosius BA (2005) Insight into the 2004 Sumatra–Andaman earthquake from GPS measurements in southeast Asia. *Nature* 436:201–206
- Yagi Y (2003) Source process of large and significant earthquakes in 2003. *Bull Int Inst Seismol Earthq Eng* v.37:145–153. <http://iisee.kenken.go.jp/staff/yagi/pdf/YagiBIISEE.pdf>